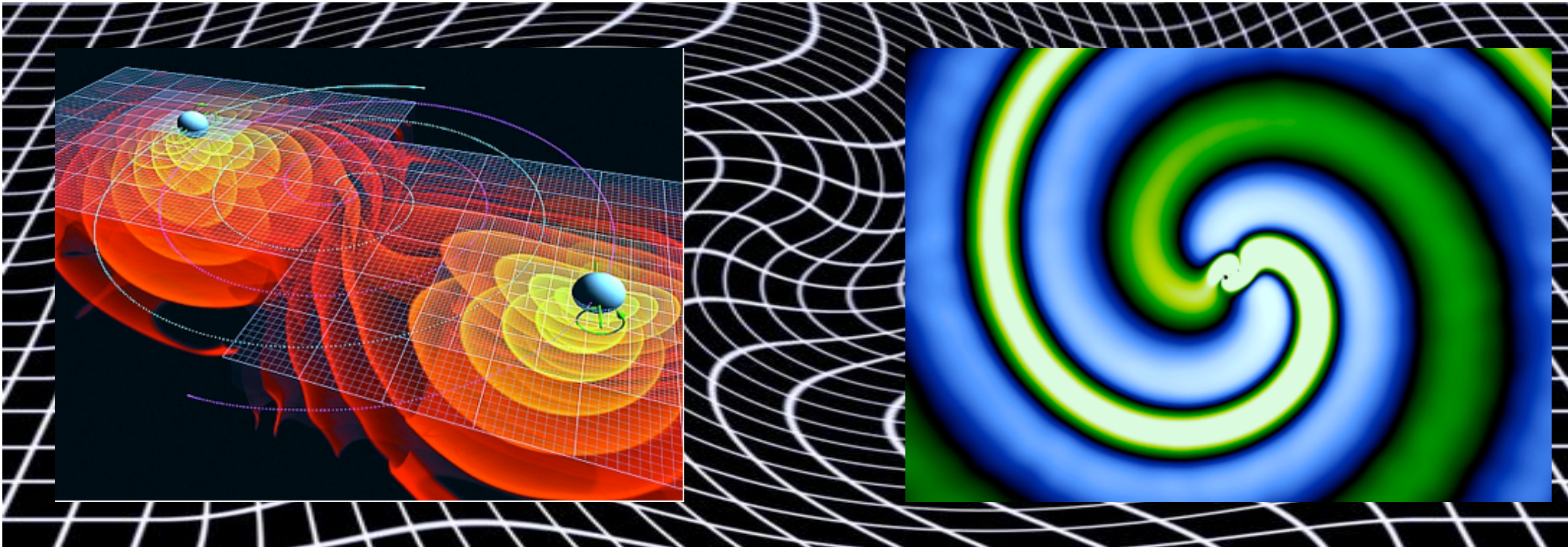


# Listening to black holes with supercomputers



General Relativity: when heavy stars run out of fuel, nothing can halt their gravitational collapse to a black hole.

Our aim: understand observational signatures of merging BH binaries, required to identify such events in gravitational wave observations.





# Thanks to collaborators and funding!

Contributors: Michael Pürerer, Mark Hannam, Sebastian Khan, Frank Ohme, Alejandro Bohé, Francisco Jimenez, Juan Calderon, Bernd Brügmann, Nathan Johnson-McDaniel, Denis Pollney, Christian Reisswig, Milton Ruiz, Patricia Schmidt, Marcus Thierfelder, Vijay Varma, Parameswaran Ajith.



**RHODES UNIVERSITY**  
*Where leaders learn*



**Caltech**





# The Dark Universe

- Black holes have taken center stage in astrophysics & fundamental physics.

- Extraordinarily clean systems, described by their mass  $M$  and spin  $\chi = \frac{|\vec{J}|}{M^2}$

- Allow precision astrophysics and fundamental physics:

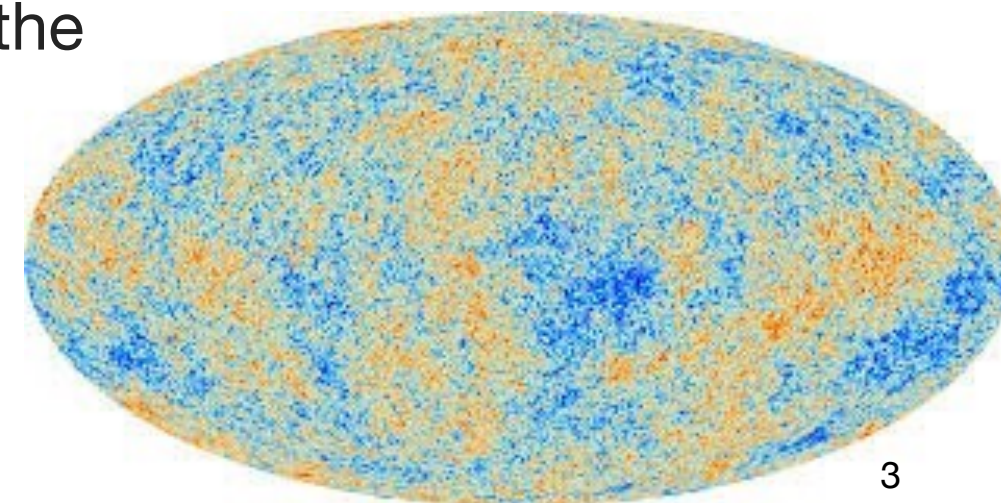
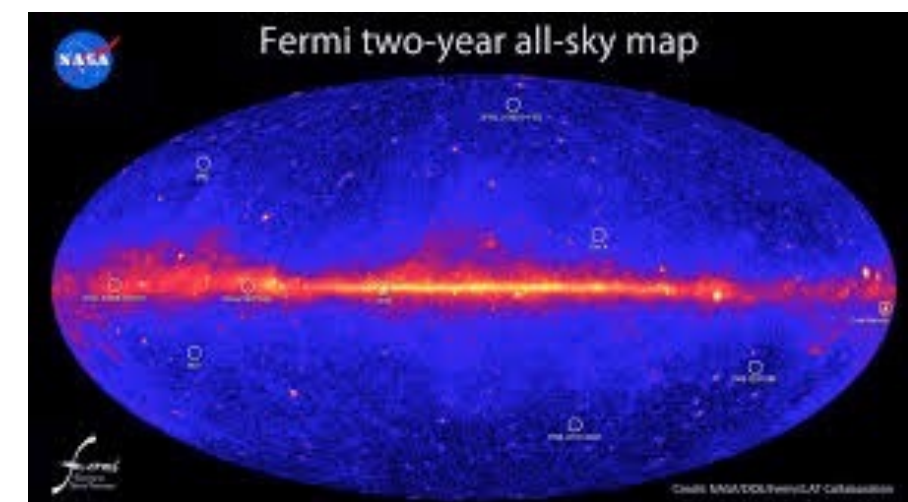
- life cycle of stars
- supermassive black holes in galaxy cores
- testing general relativity - find new physics?

- direct observation?

- Electromagnetic waves taught us what we know about the universe. Superposition of waves from many particles

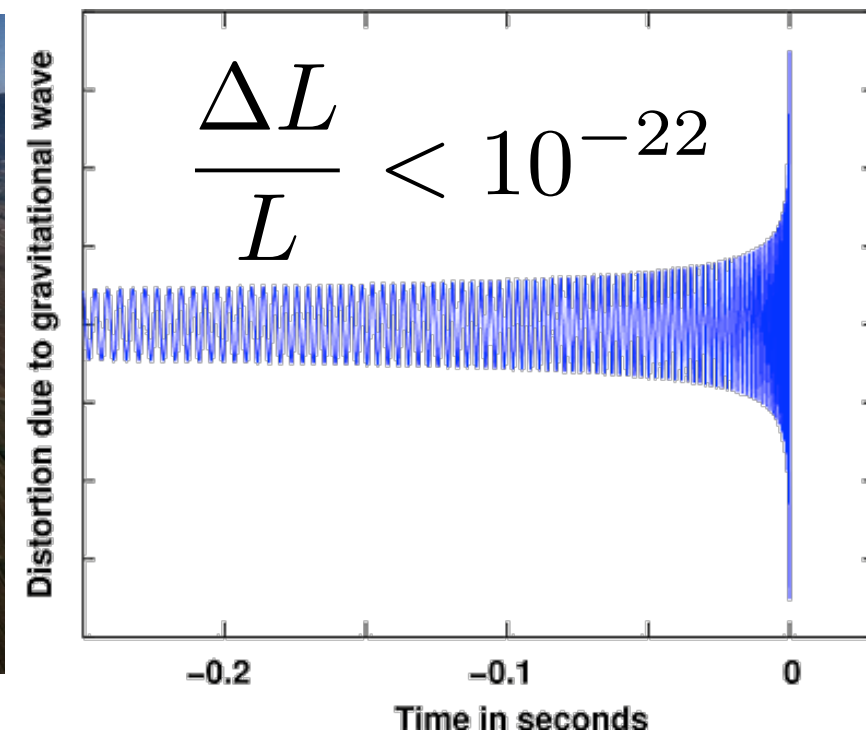
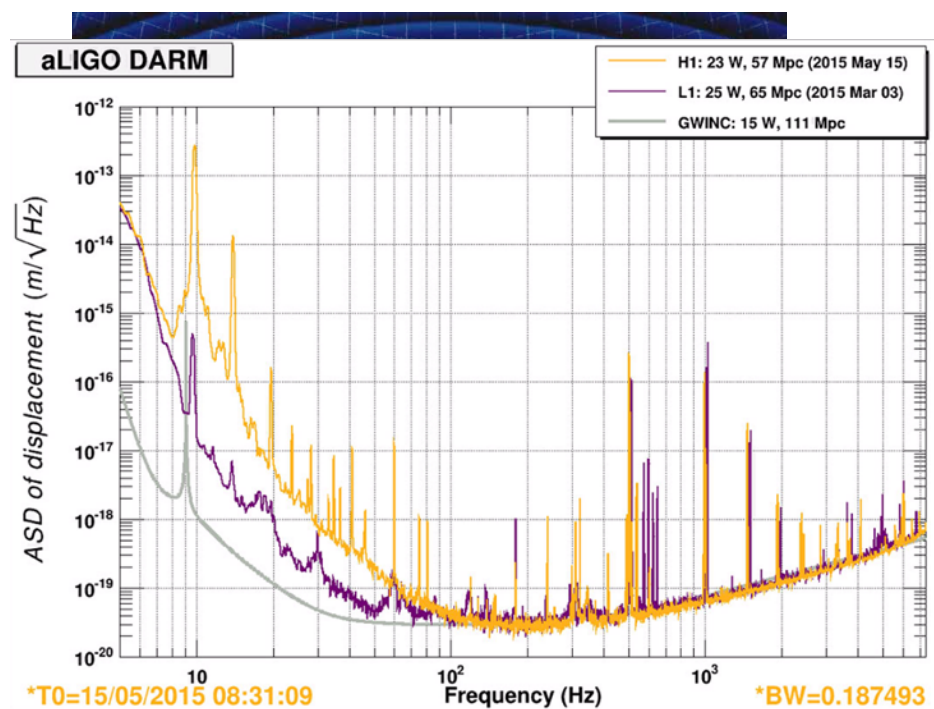
- —> image of the source.

- Electromagnetic spectrum is blind to some of the most violent and exotic objects in the universe.



# Gravitational Waves

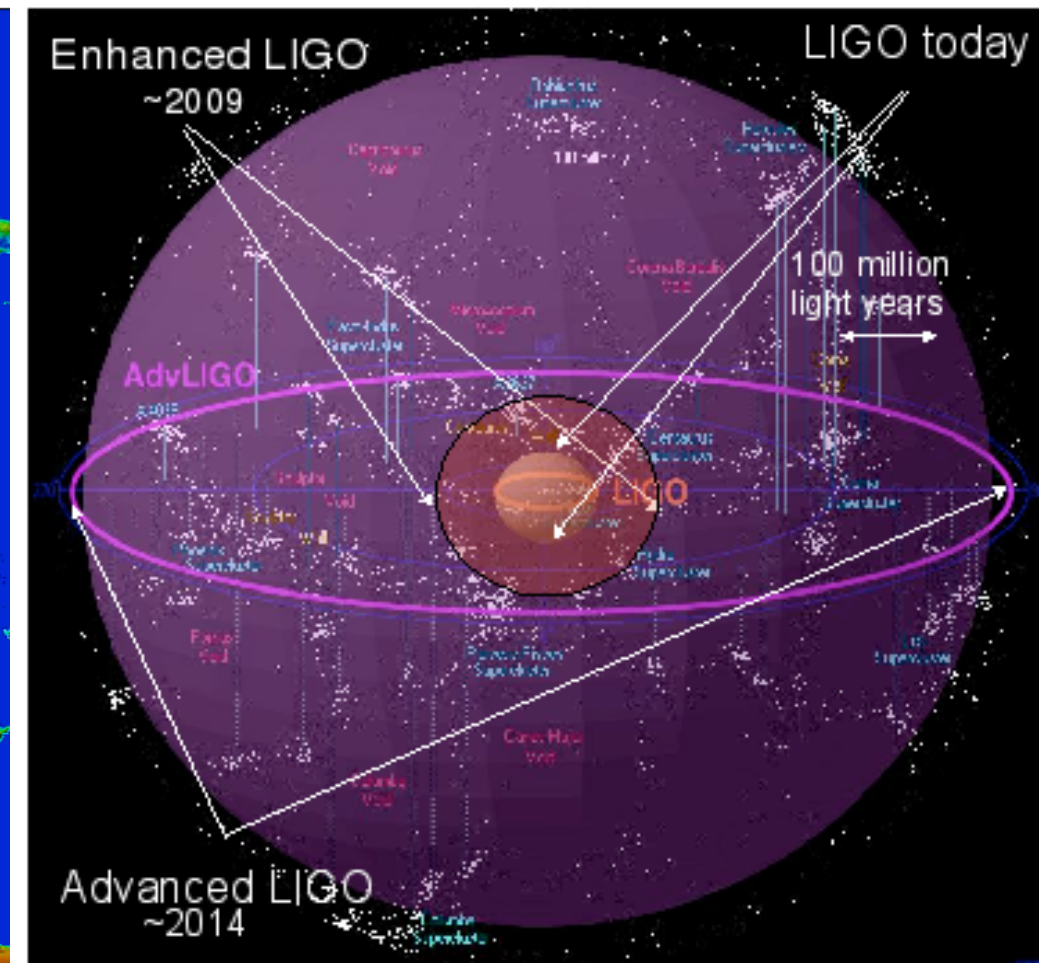
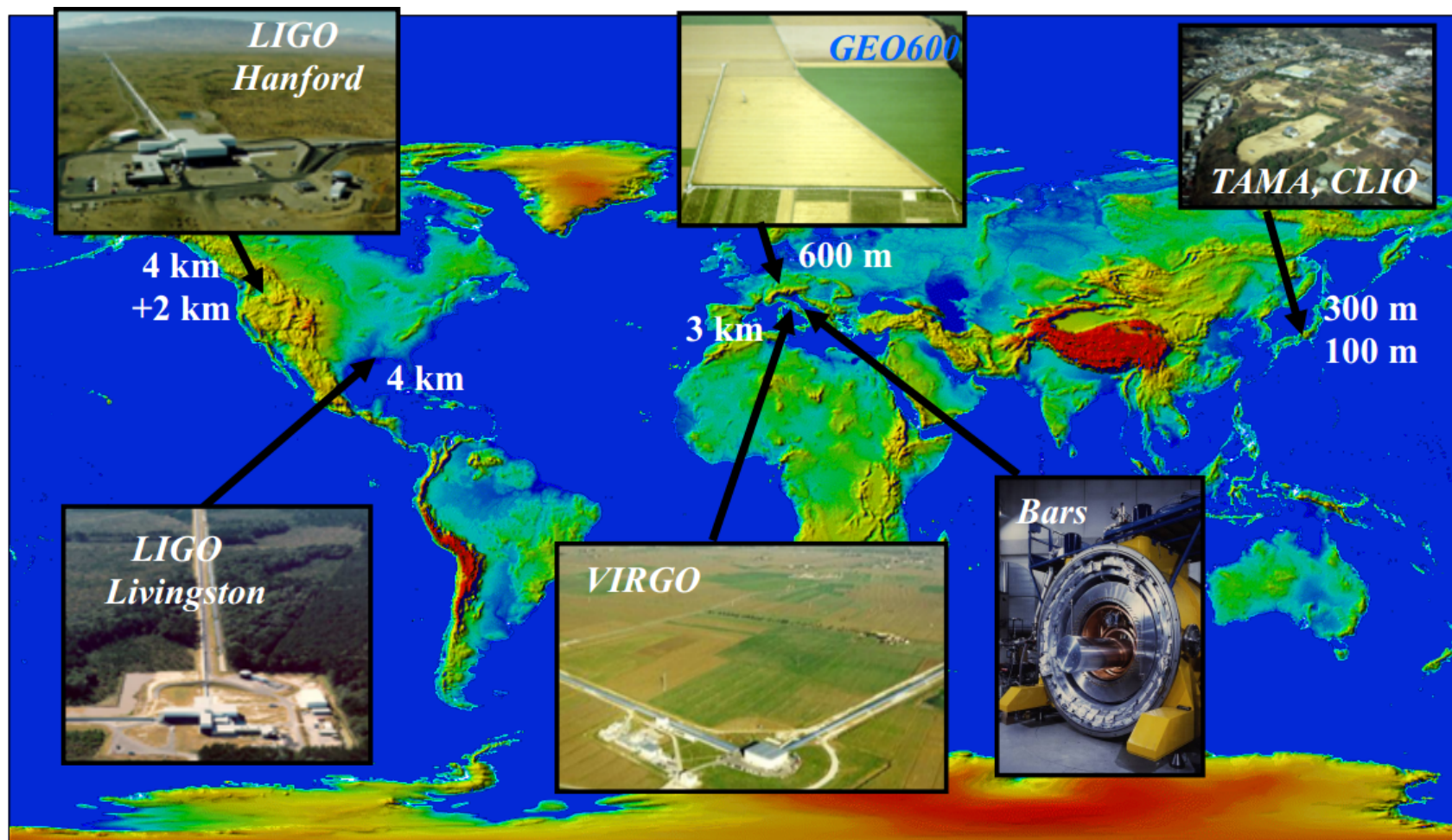
- Spacetime in general relativity is a deformable entity, ripples in spacetime travel at the speed of light and carry with the information on their source.
- Close binary systems of BH/NS are most efficient sources of gravitational waves.



- GW signal carries information about the bulk motion of objects: analogous to hearing sound.
  - “soundtrack of the universe”
- GW signal encodes masses, spins, eccentricity of binary & possibly new physics - needs to be decoded.



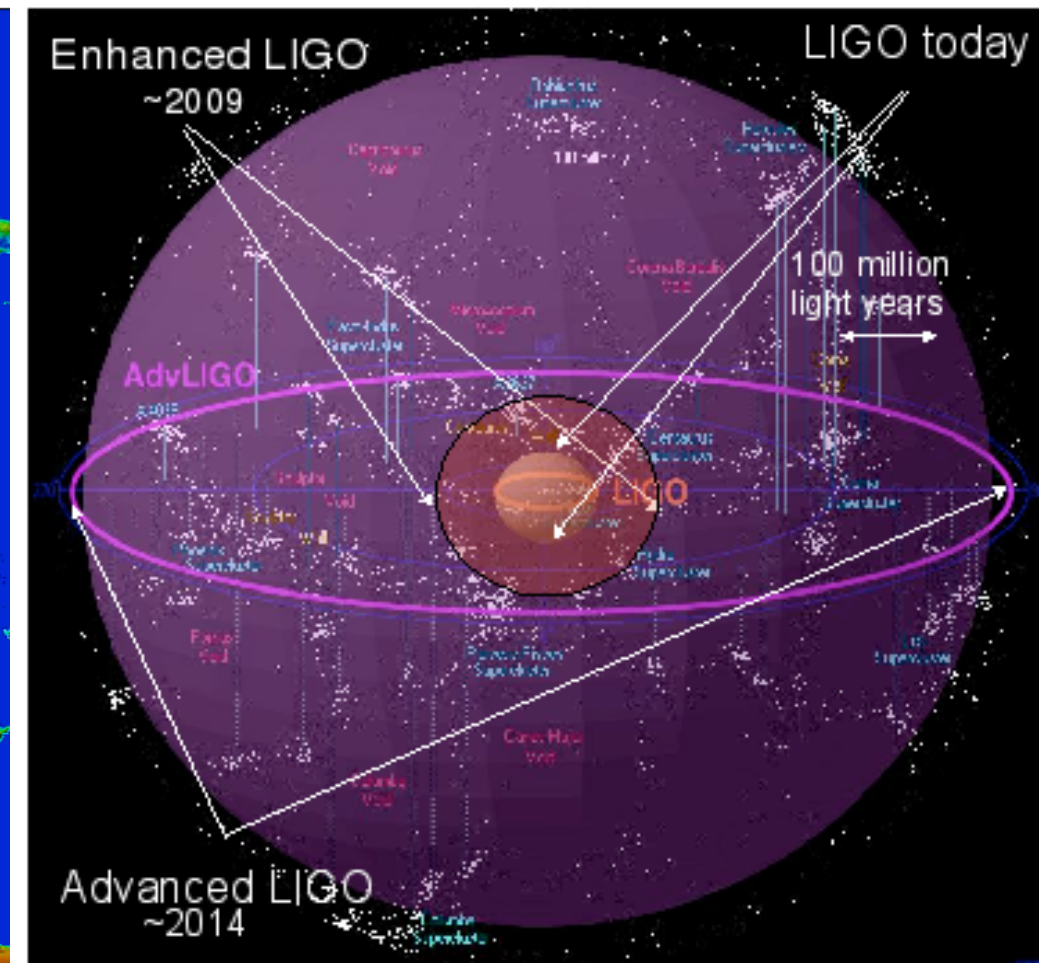
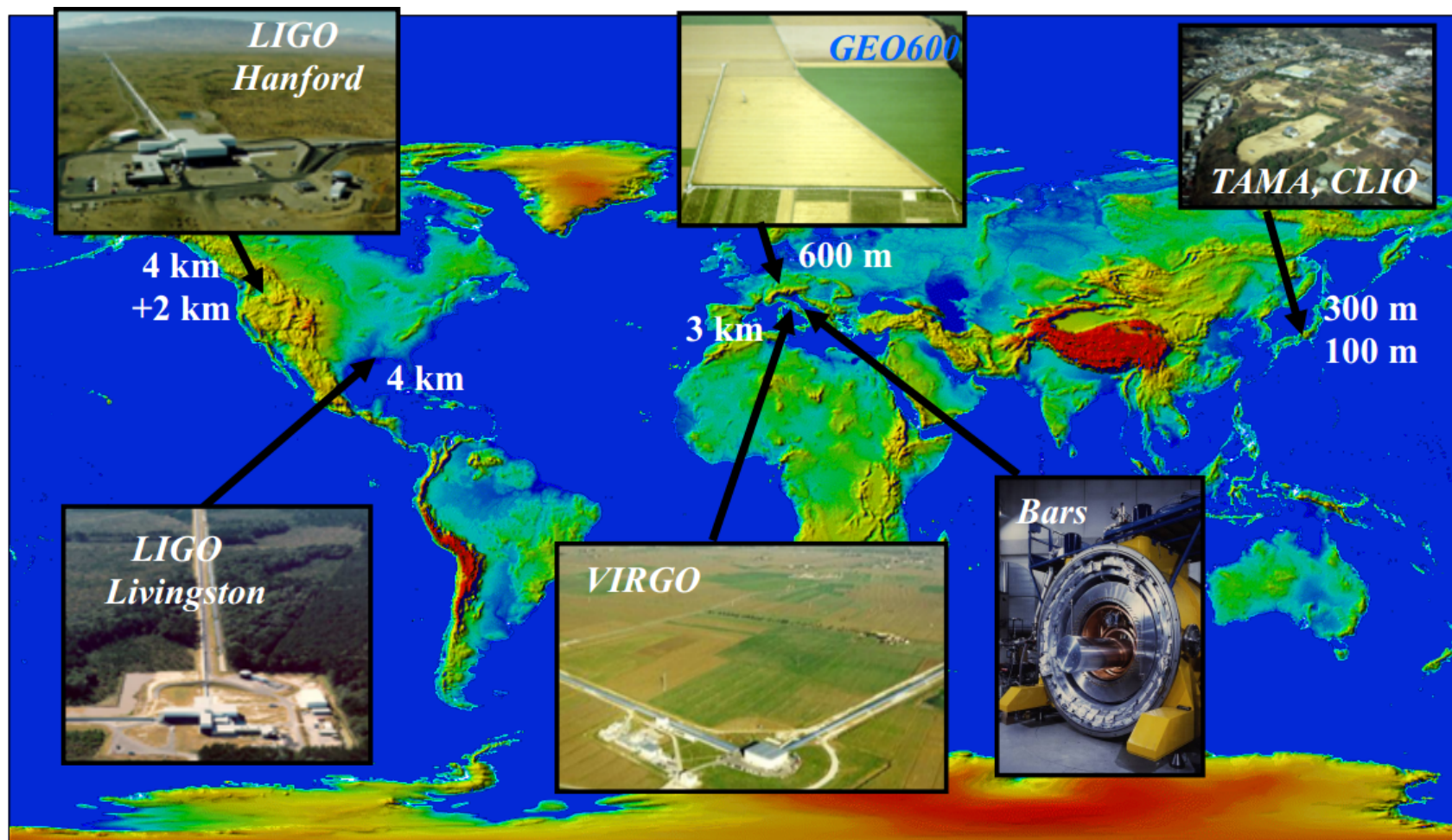
# Gravitational wave detectors and data analysis



- Since first LIGO science run in 2002 upper limits have been set, but no direct detection, LIGO-Virgo Scientific collaboration has grown to ~ 1000 scientists.
- Computational challenge 1: Searches for BH merger events are based on “matched filtering” with template waveforms.
- Computational challenge 2: “template banks” need to be computed in general relativity - Inaccurate templates: lose events & incorrectly identify them (masses & spins of a binary, identification as BH or NS).



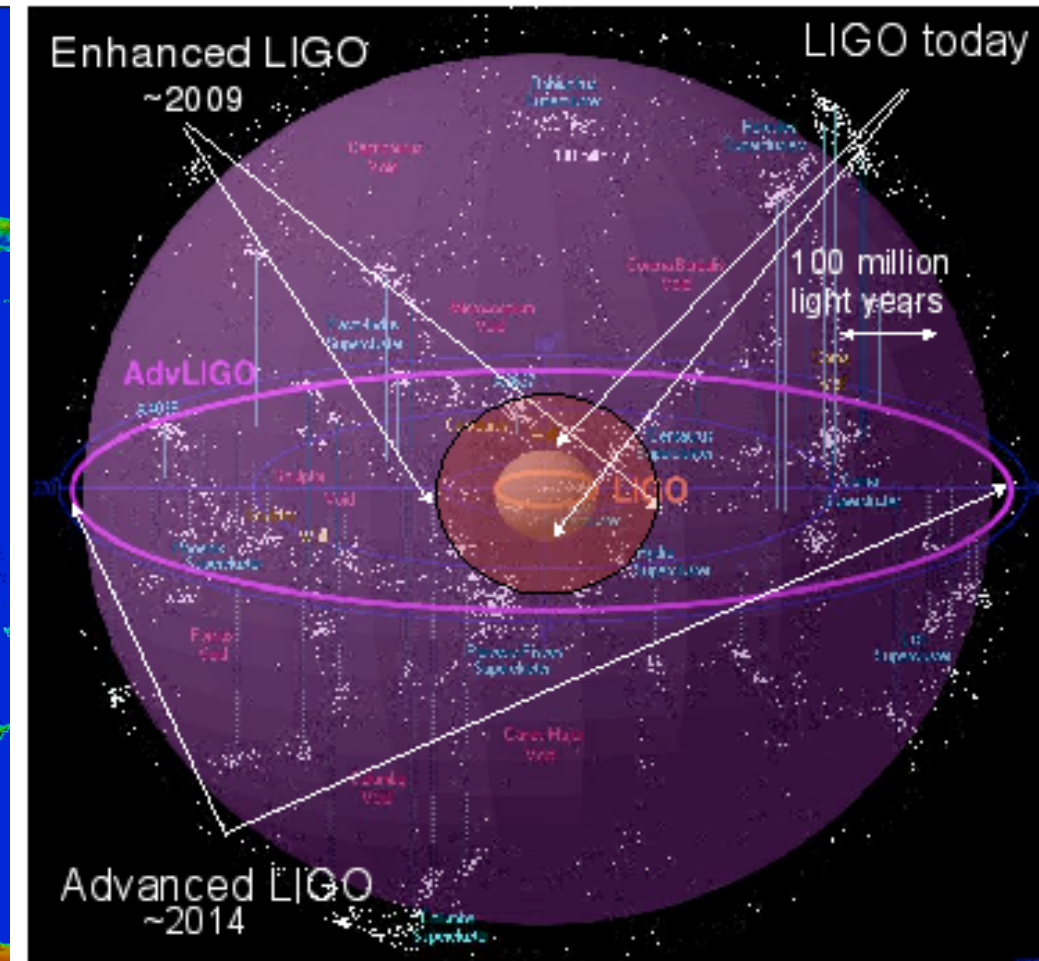
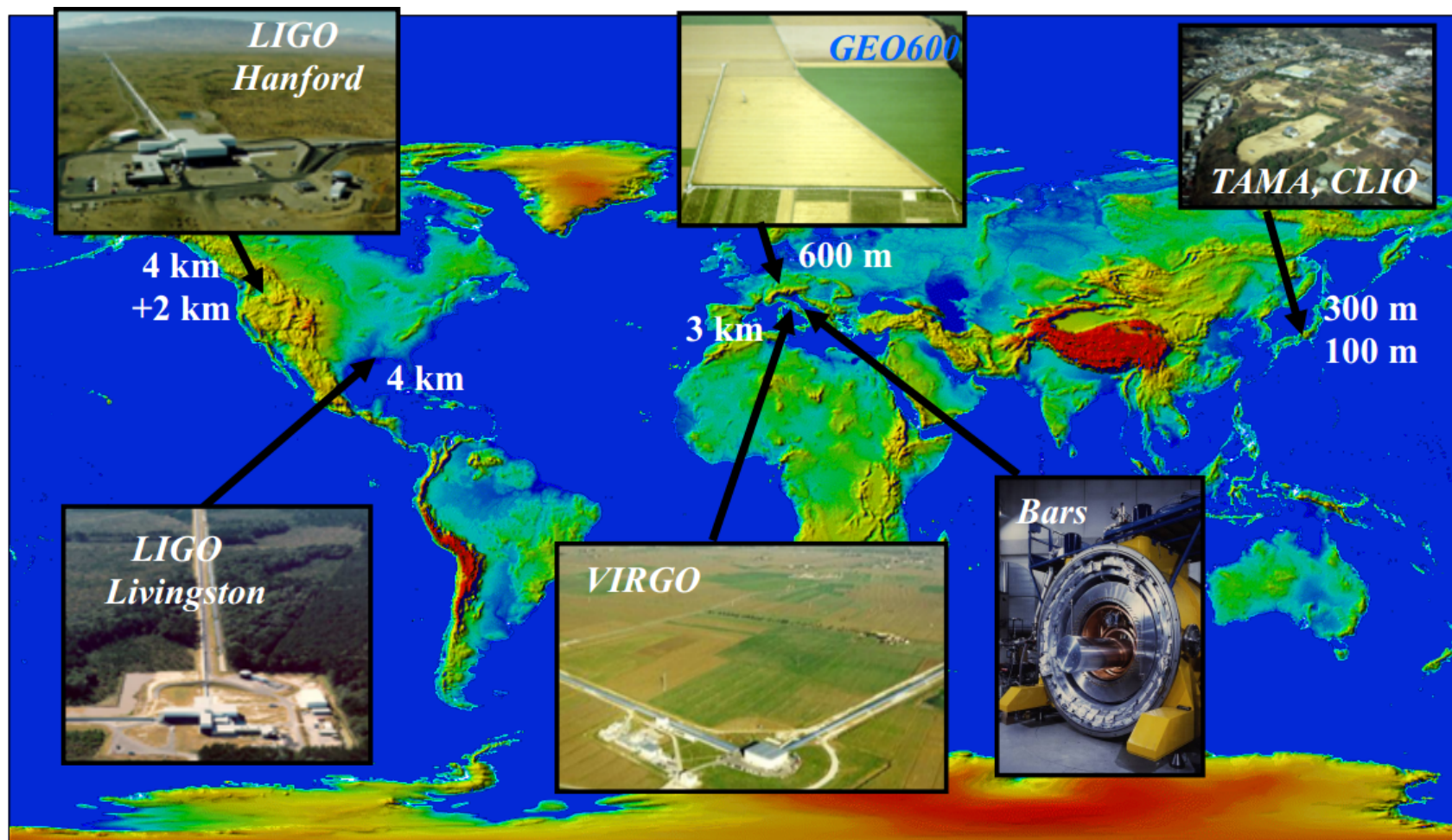
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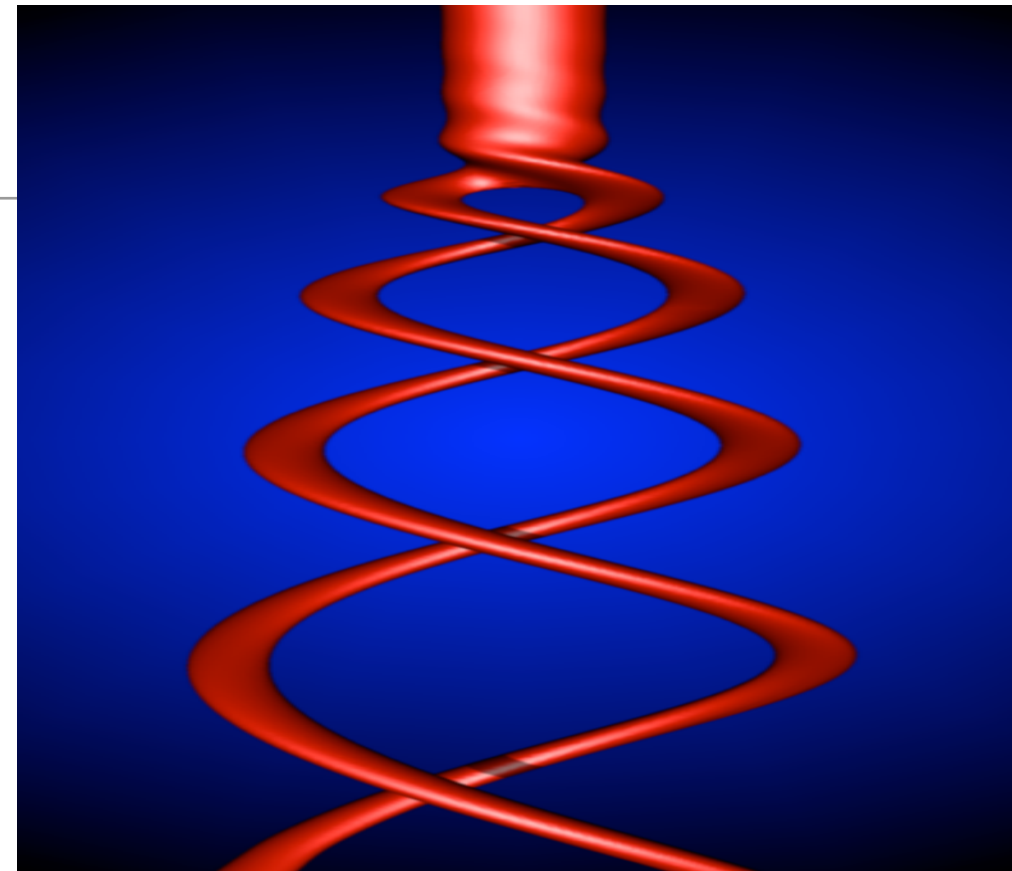
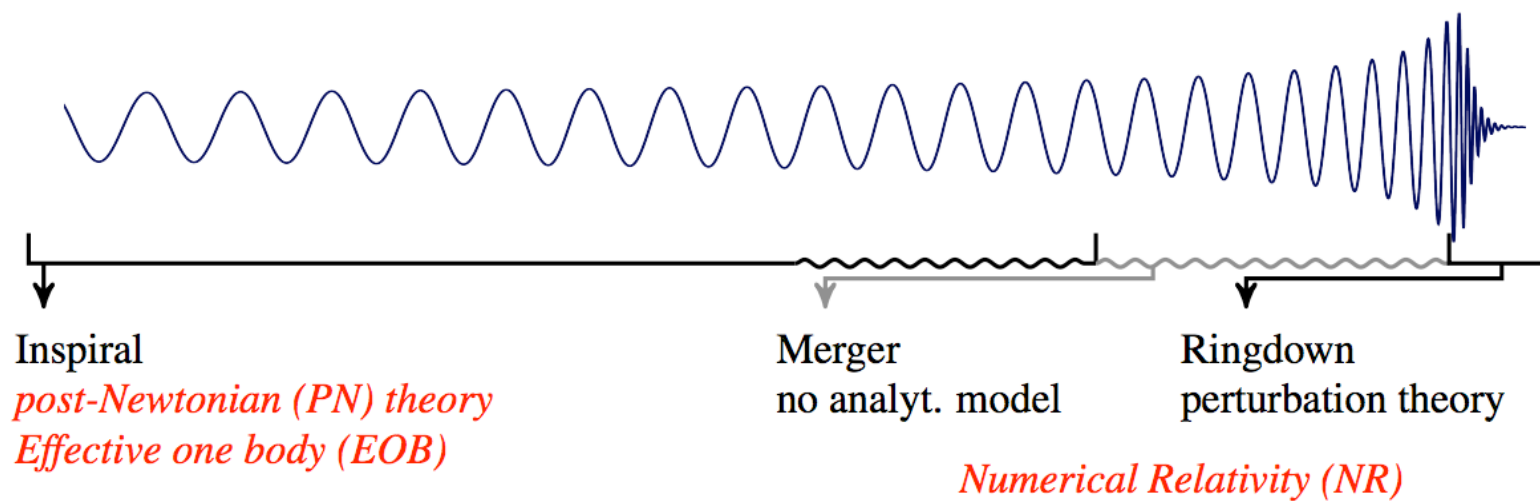
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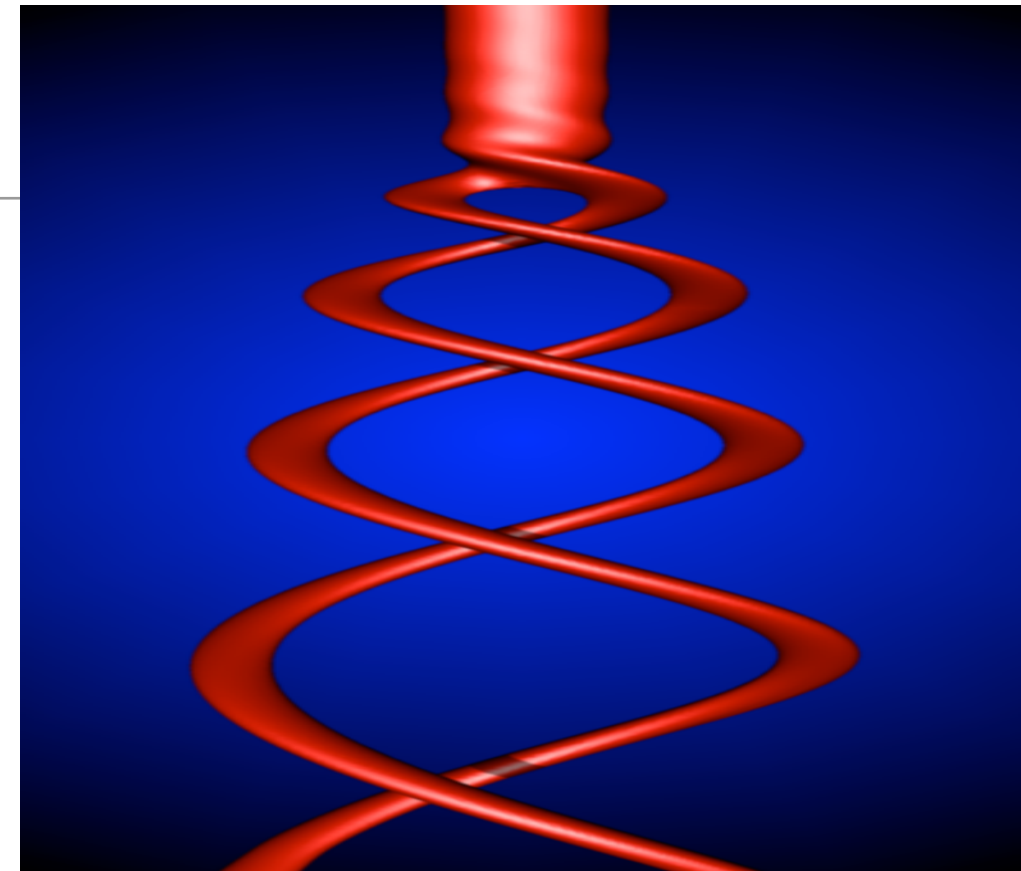
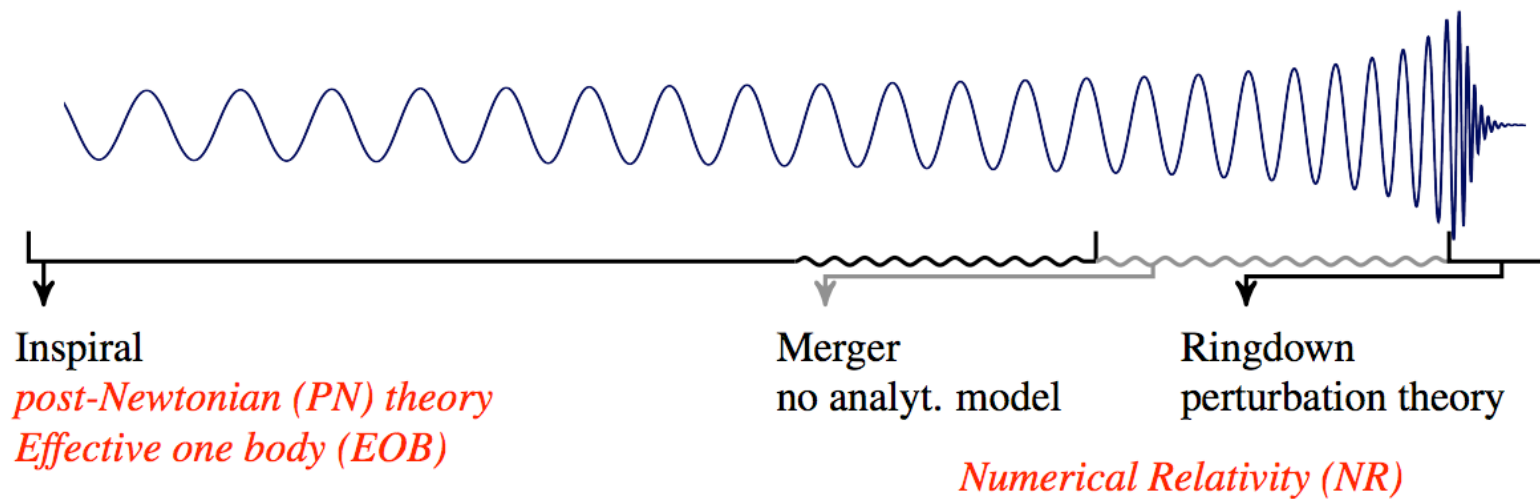
# Anatomy of BH mergers



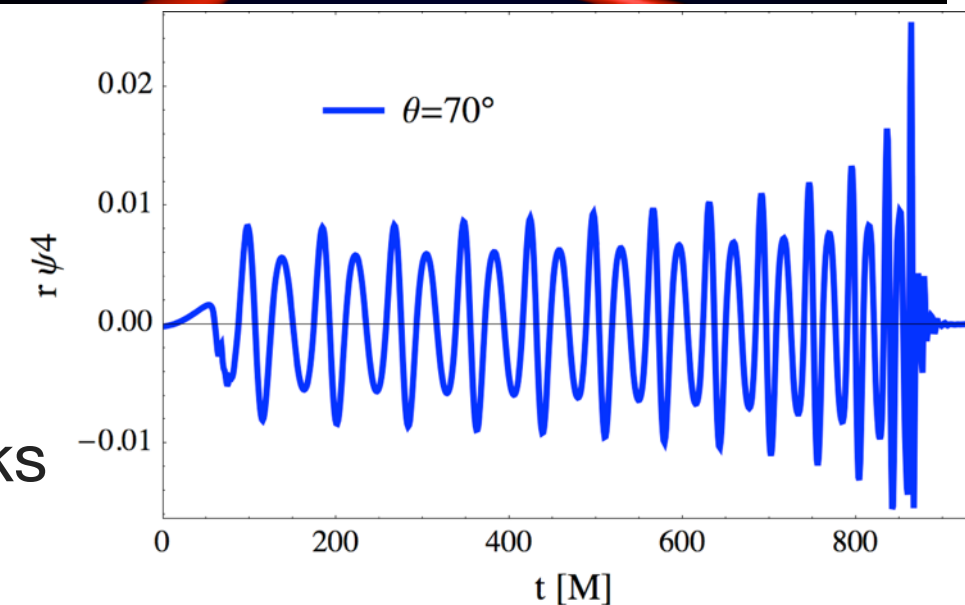
- Inspiral: energy loss to GWs leads to adiabatic inspiral, well described by post-Newtonian perturbation theory.
- Late inspiral & merger: post-Newtonian expansion breaks
  - solve full Einstein equations numerically as PDEs, “match” to post-Newtonian inspiral.
  - Most of the energy released ( $< 12\%$  of the mass).
- Ringdown: superposition of damped harmonics, frequencies known from perturbation theory.



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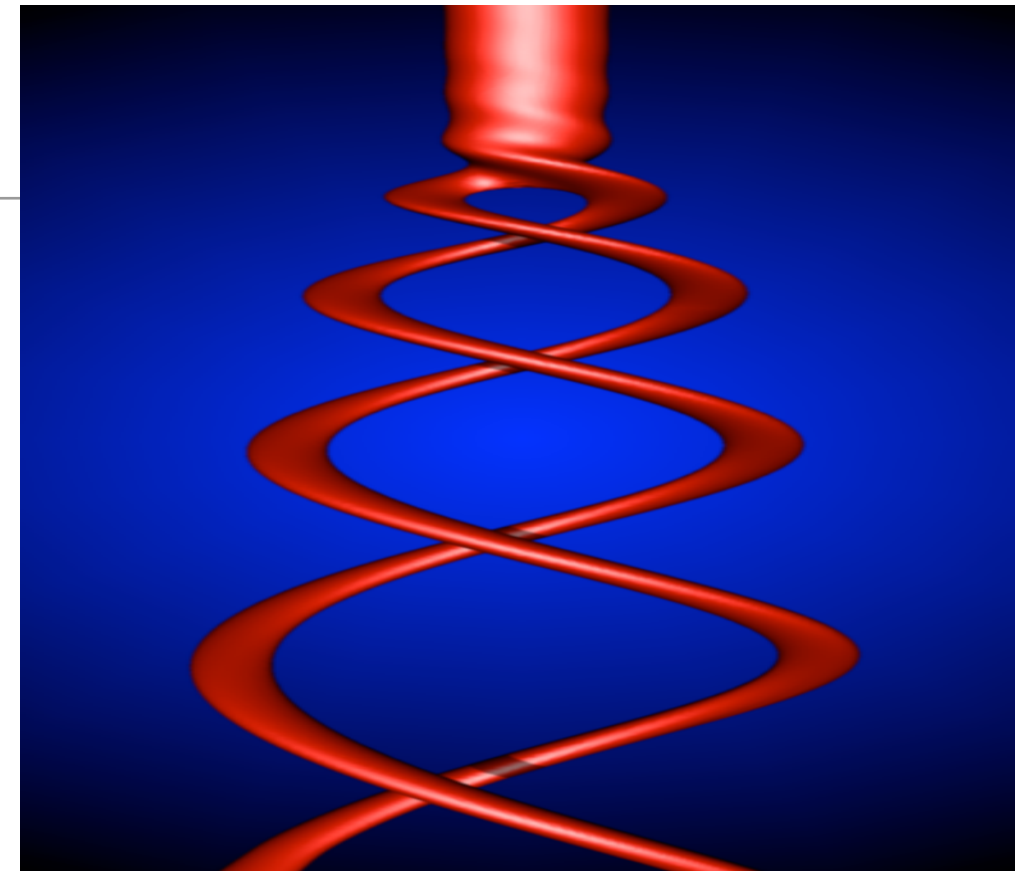
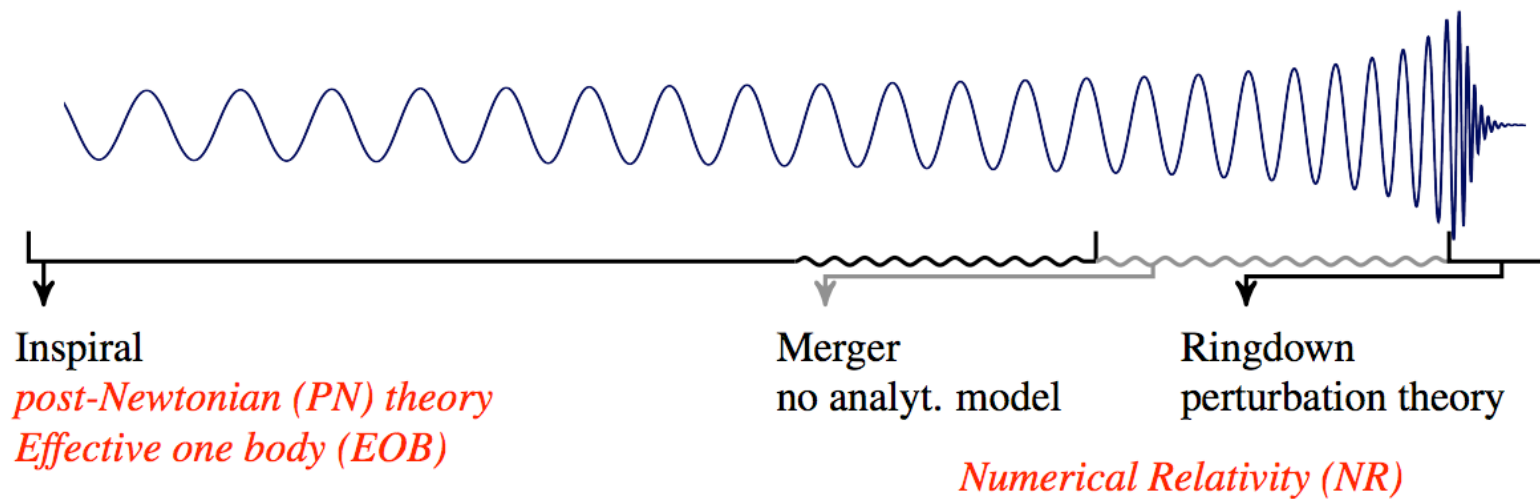


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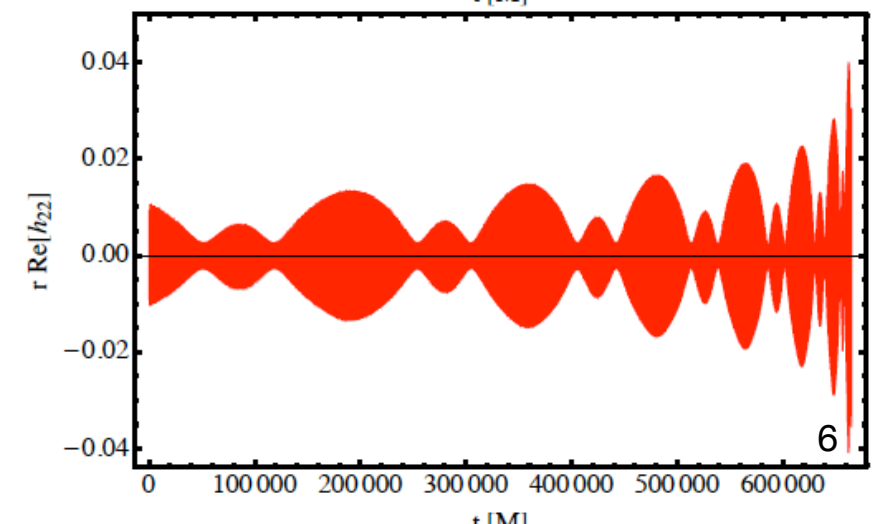
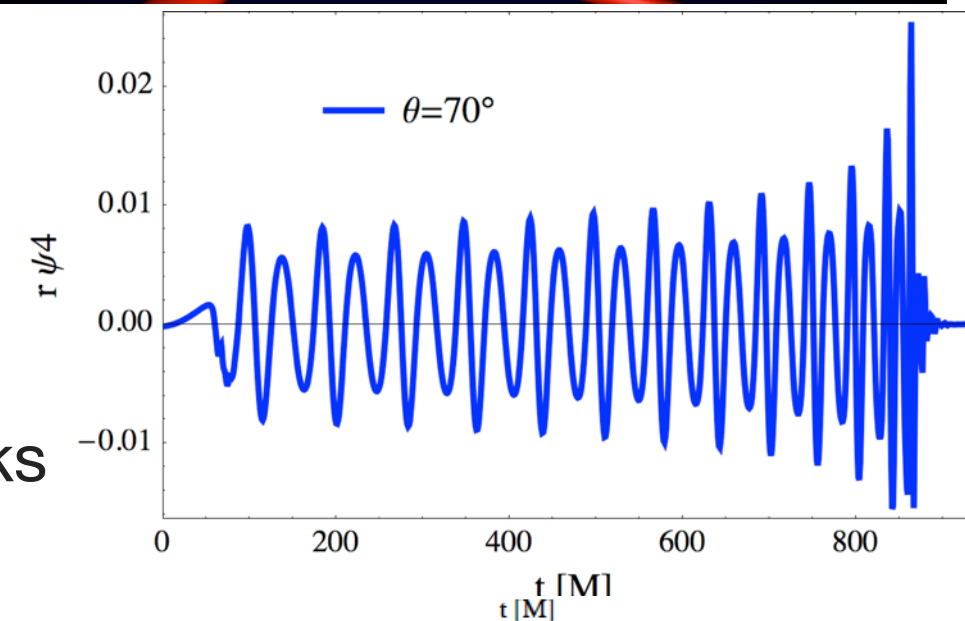




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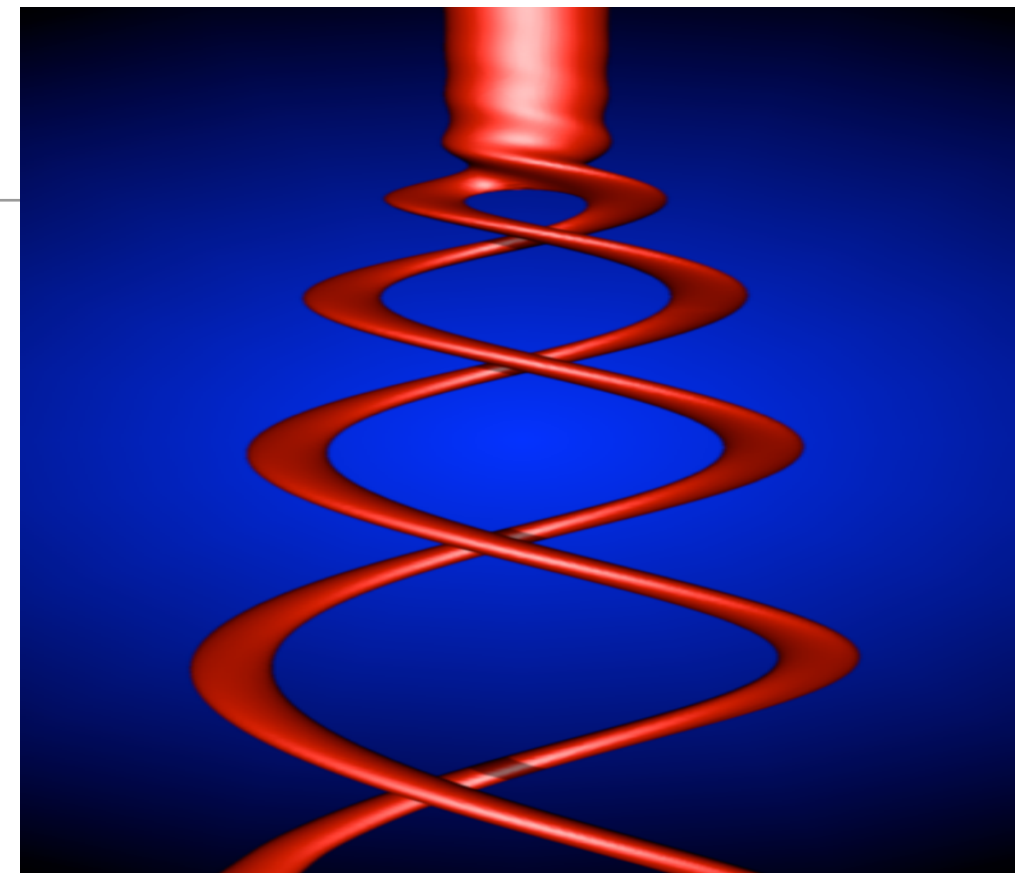
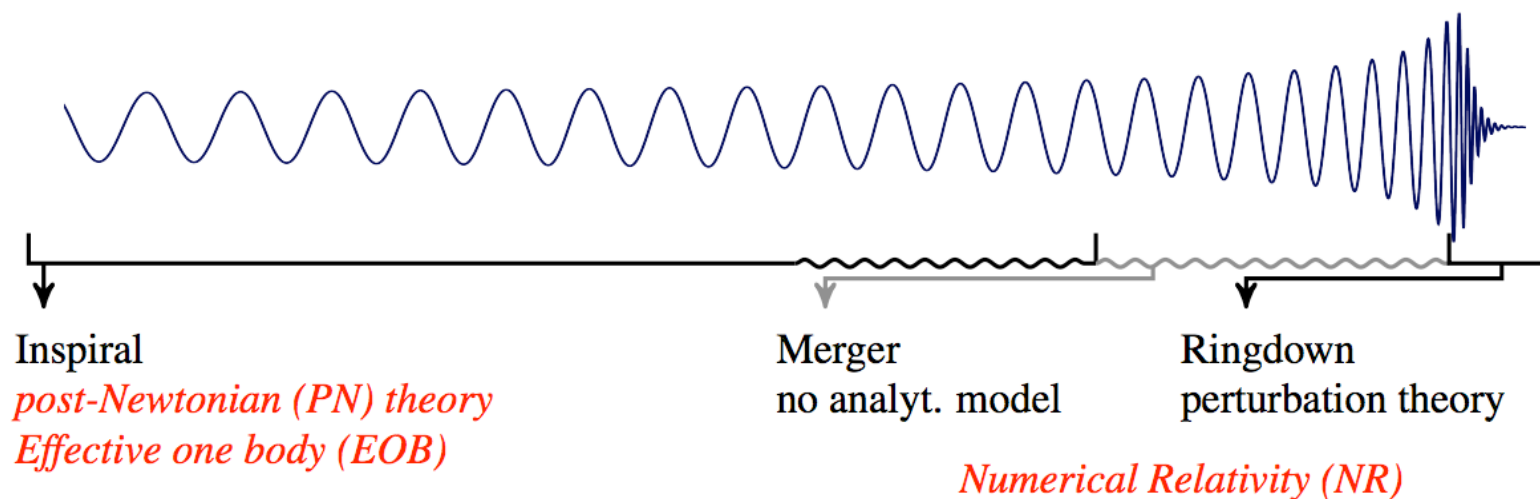


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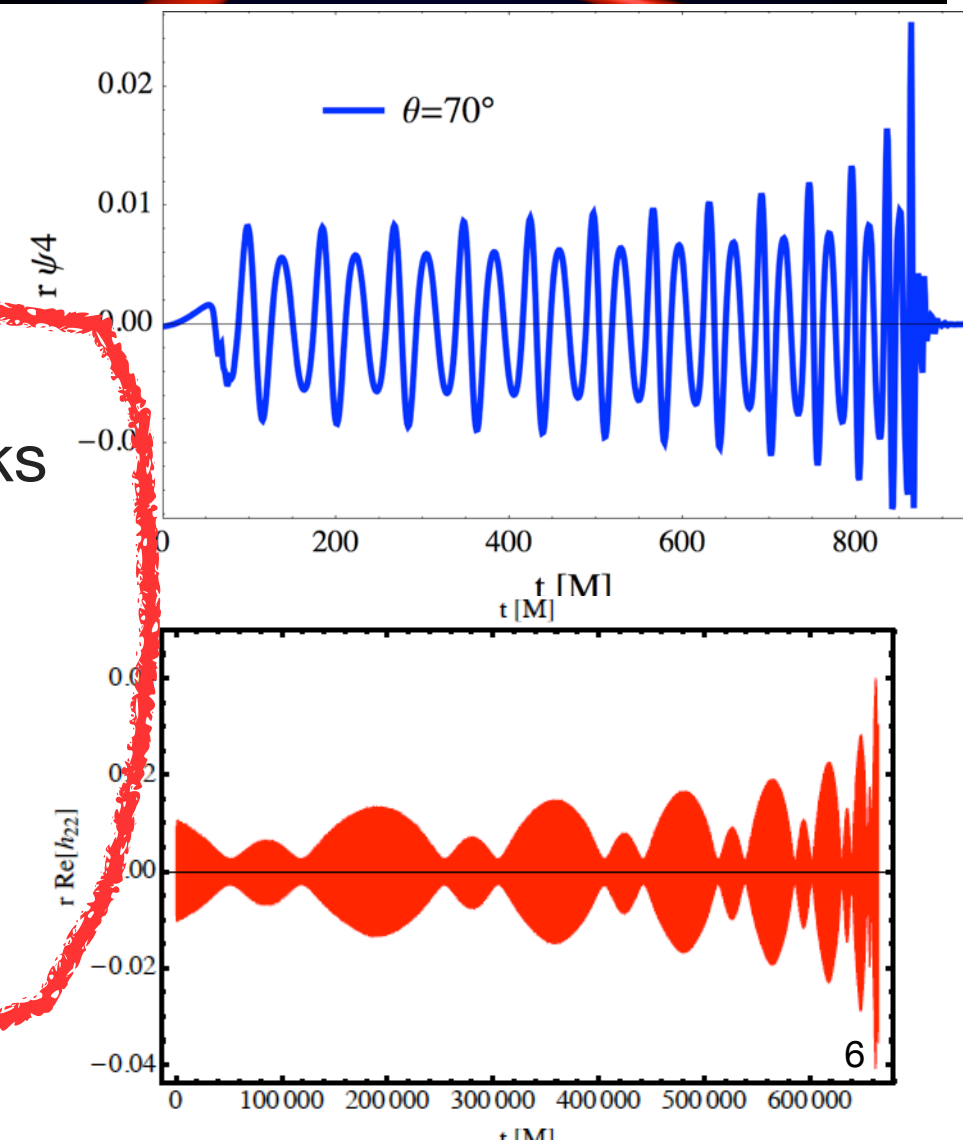


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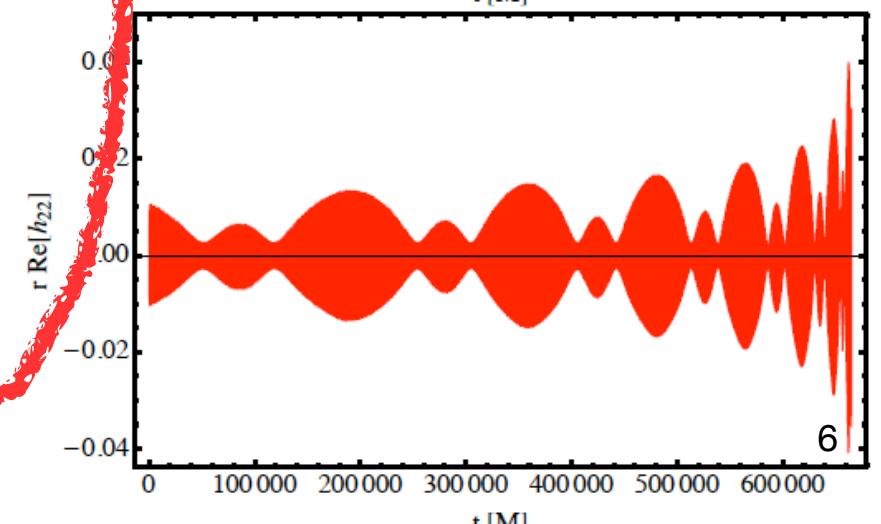
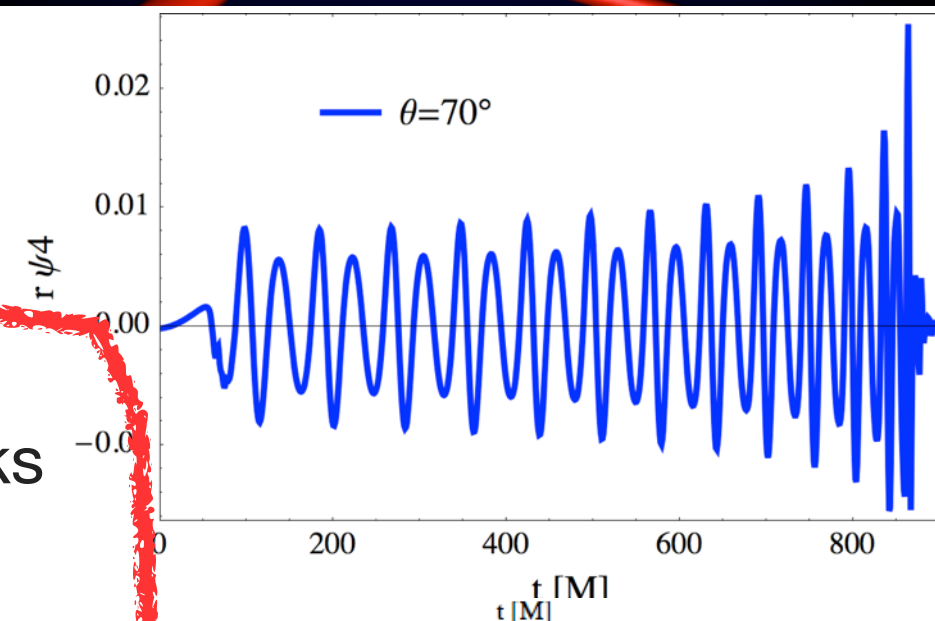
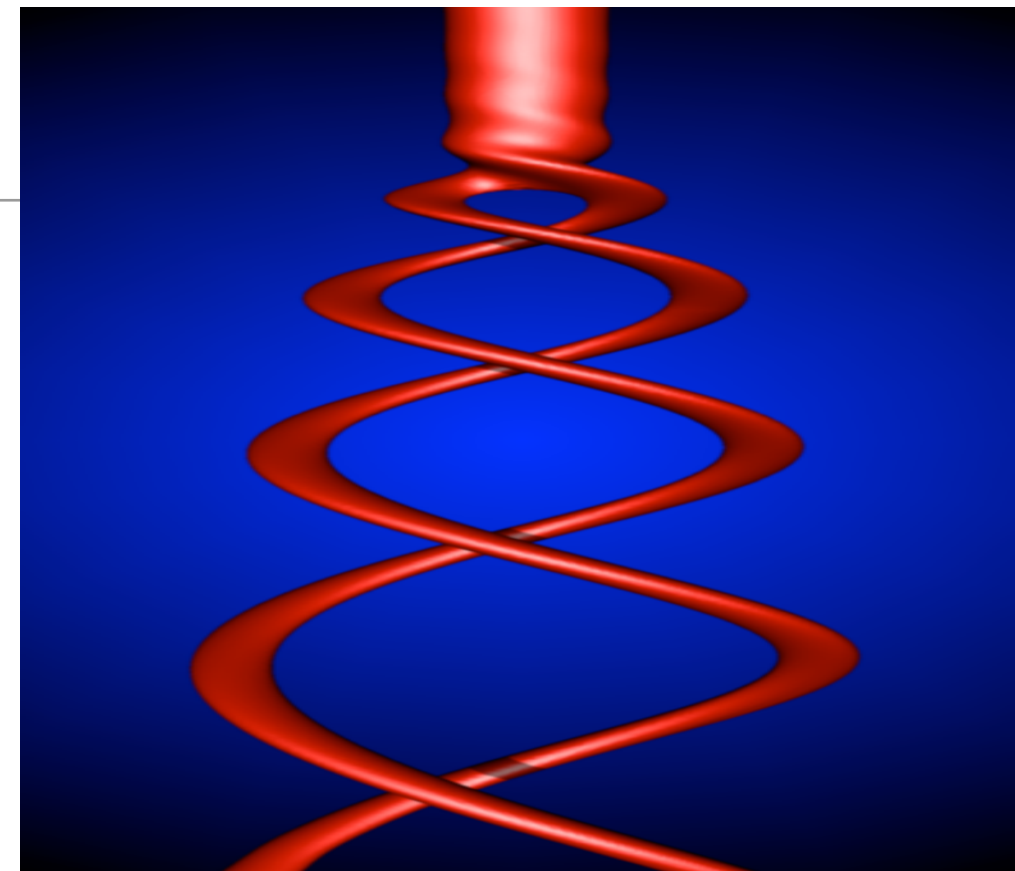


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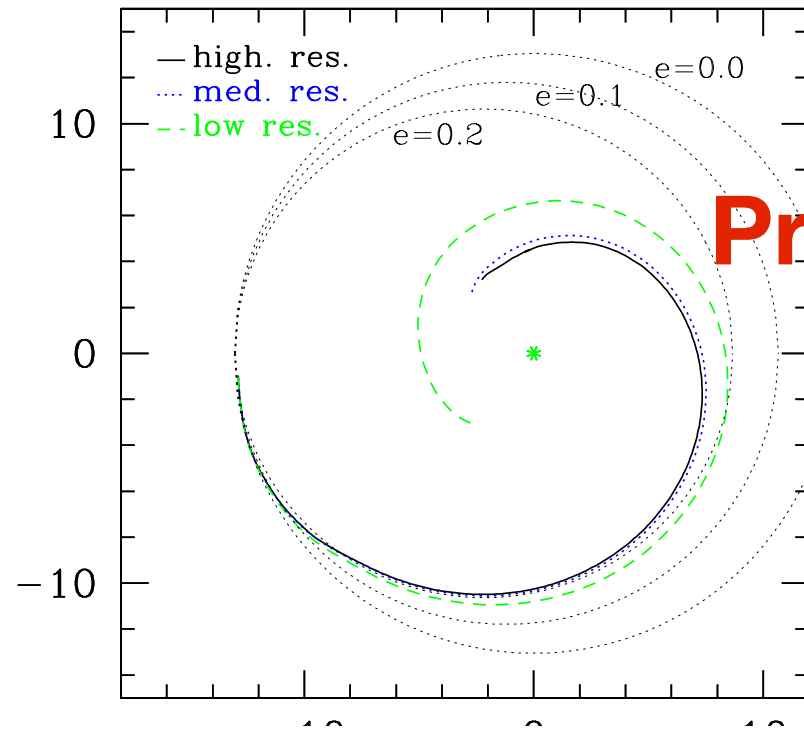
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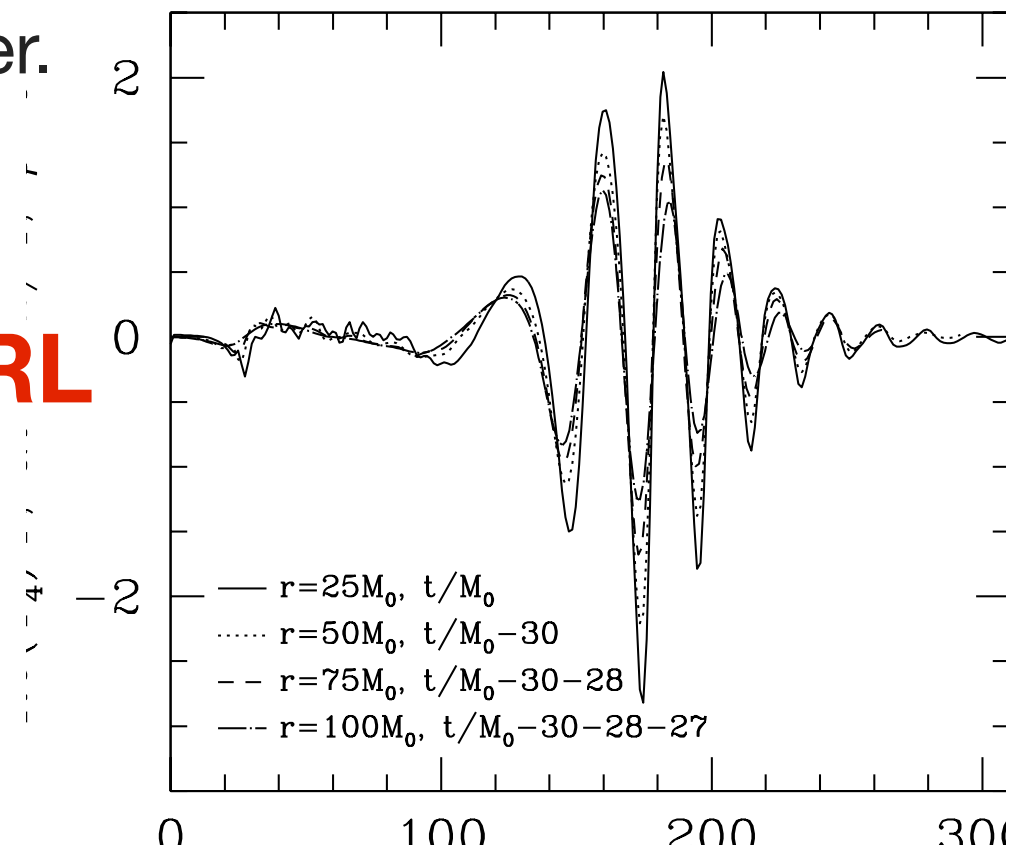


# Solving the Einstein equations

- Einstein equations describe geometry of spacetime, not fields on a fixed spacetime -> technical problems took 4 decades to solve for 2-body problem.
- EE can be viewed as 10 coupled nonlinear wave equations (hyperbolic) plus elliptic constraint equations (solved initially, then just monitored).
- We evolve BSSNOK version: 24 evolution equations + monitor 9 constraints.
  - 1000s of terms, hard to optimize for compiler.



**Pretorius 2005 PRL**

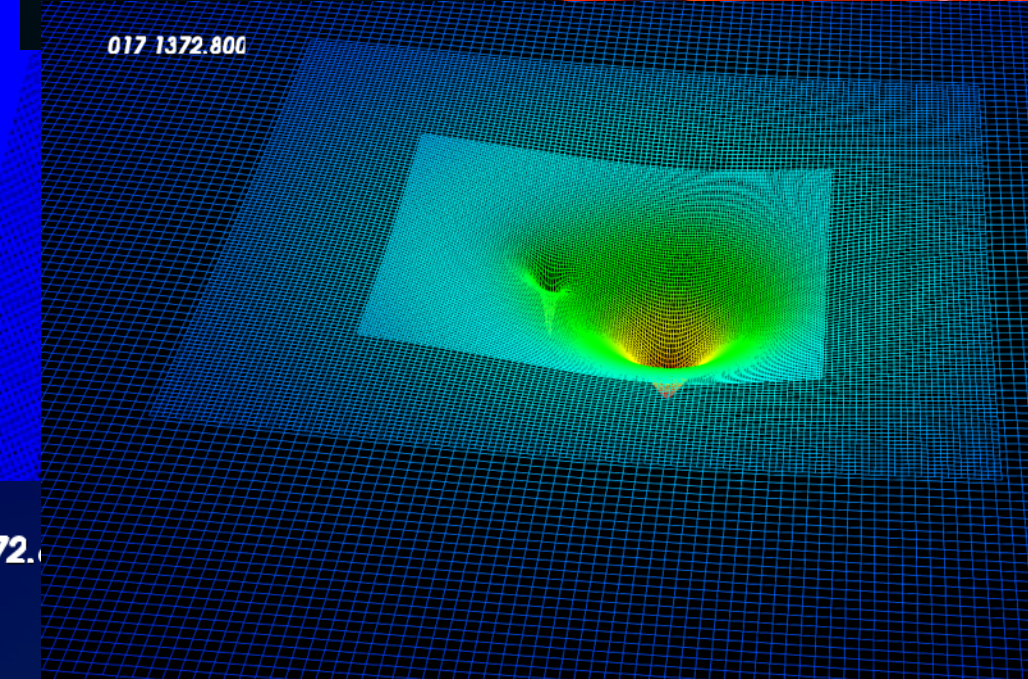
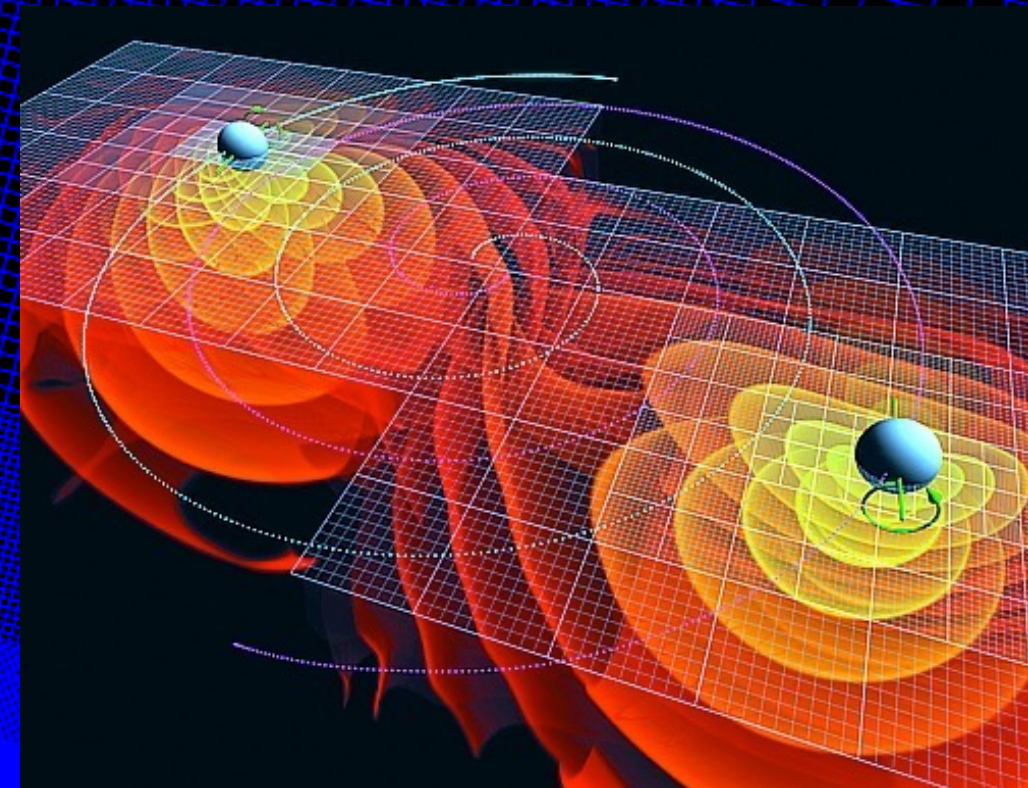


- Einstein equations form singularities hidden inside BHs, not shocks -> use 6-8th order finite differencing. More efficient, but less robust: spectral.



# Scales and mesh refinement

- BH binaries have several length & time scales:
  - individual BHs (most compact objects)
    - resolution around BHs determines accuracy of tracking orbital phase
  - “recipe” to configure box sizes
  - orbital scale: typically start at separations  $> 15 \text{ km } M/M_{\text{sun}}$
- wave scale frequency increases  $\sim$  factor of 10
- $1/\text{distance}^n$  background falloff
- ambiguity in boundary conditions:
  - causally isolate boundaries
    - $\rightarrow 1000\text{s of km } M/M_{\text{sun}}$

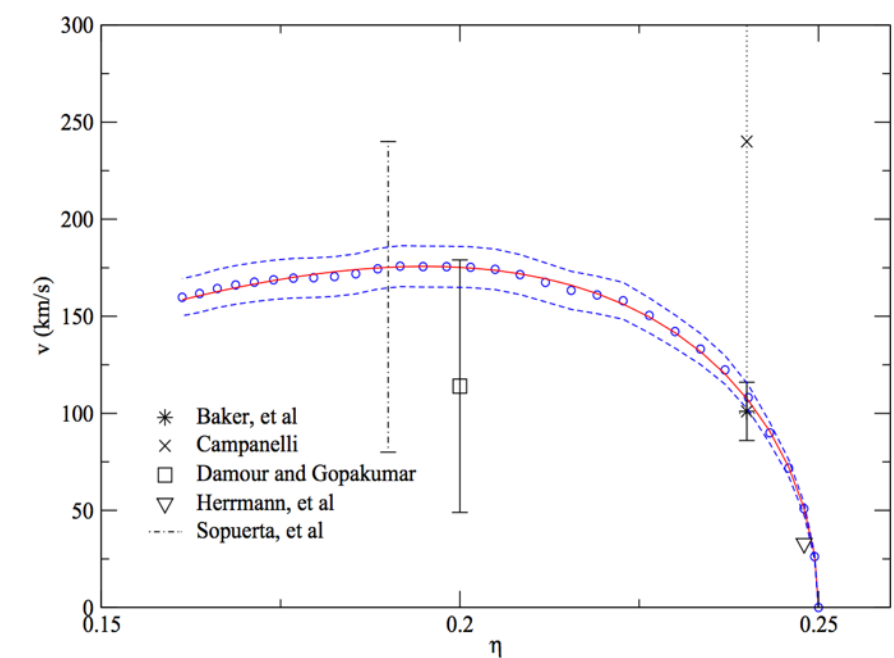


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# Project History & Strategy

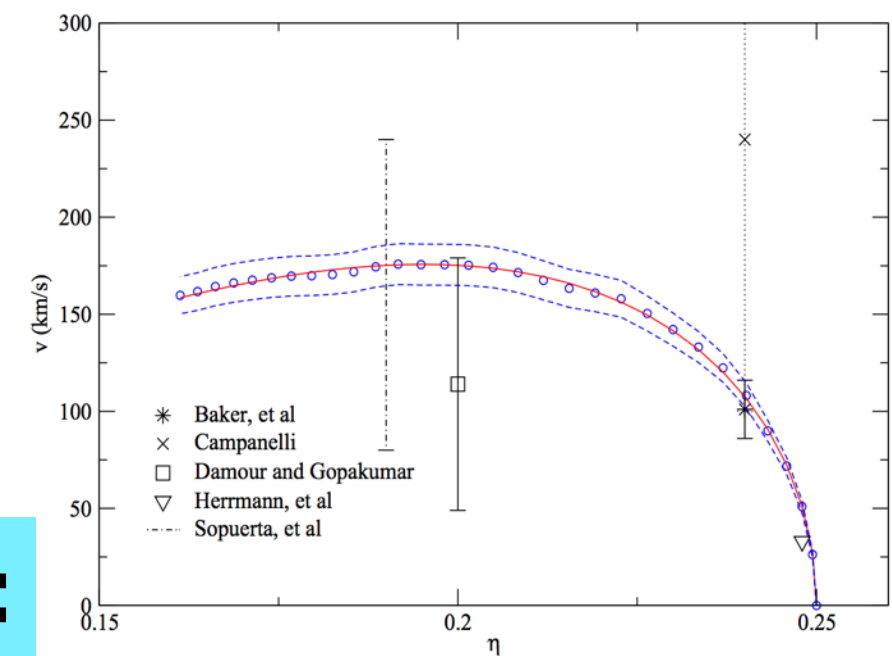
- 2006: Uni Jena + 1 million hours from DECI LRZ/HLRB-II + MPI Hannover/Potsdam
- **phenomenological waveform program:  
analytical waveform models in the frequency domain**
  - make use of degeneracies and hierarchy in 7D parameter space
  - robust finite difference code to explore parameter space
- 43 publications
- 16.7 + 37 million hours in PRACE 3+5, waiting for current evaluation
  - need hundreds of cases @  $10^4$  -  $10^6$  CPU hours to ensure detection and parameter estimation ~100s of million of CPU hours.
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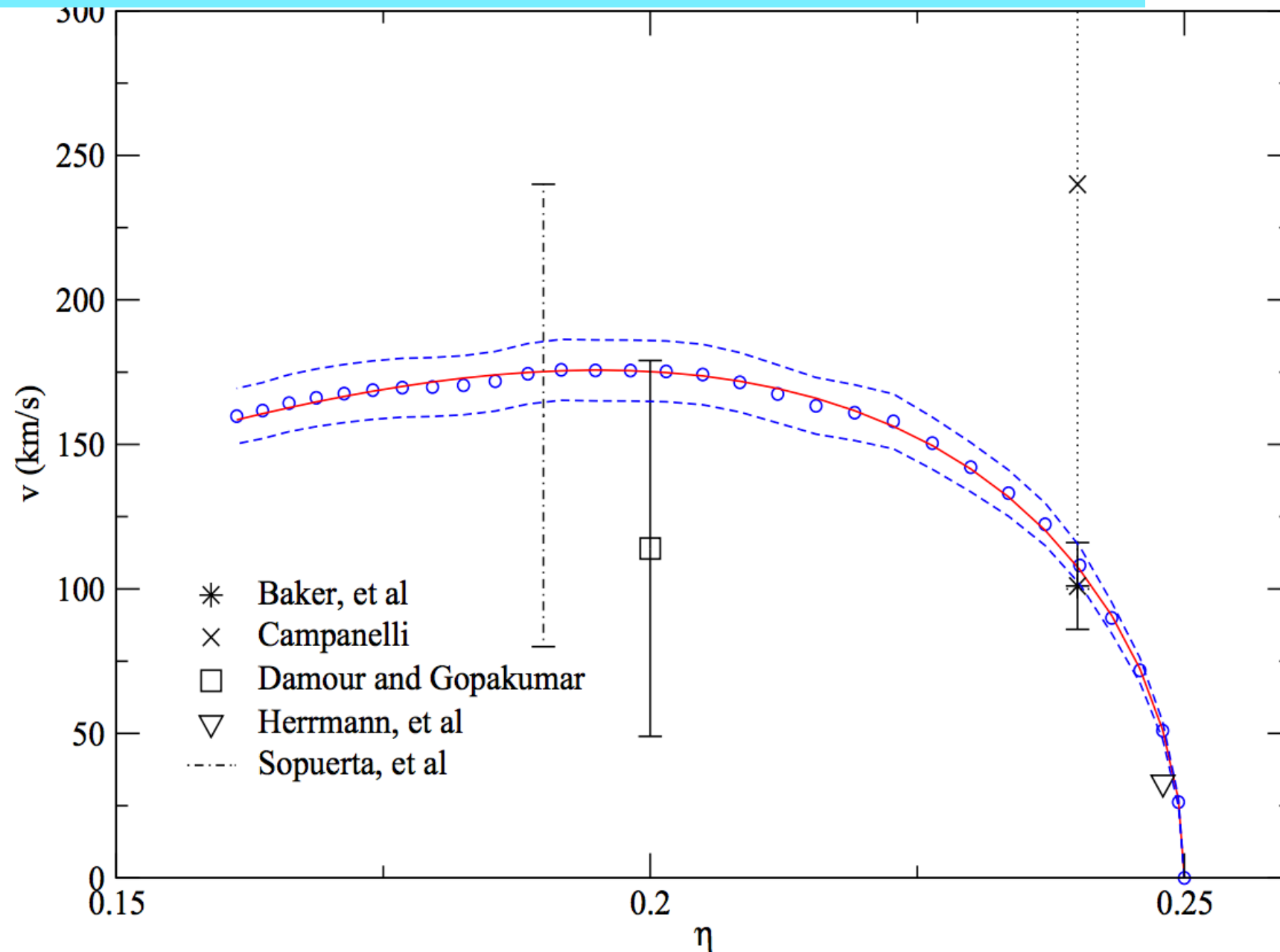
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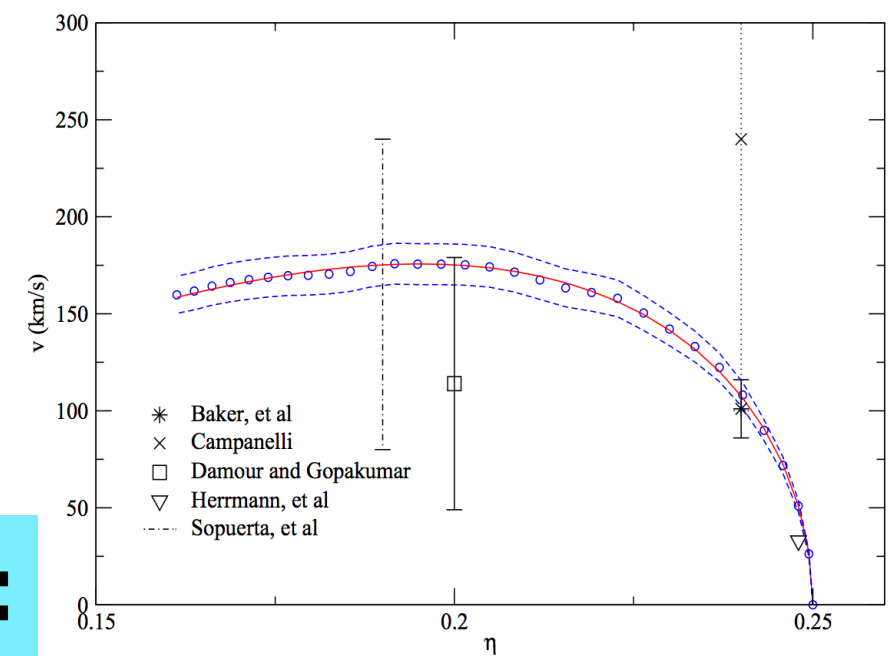
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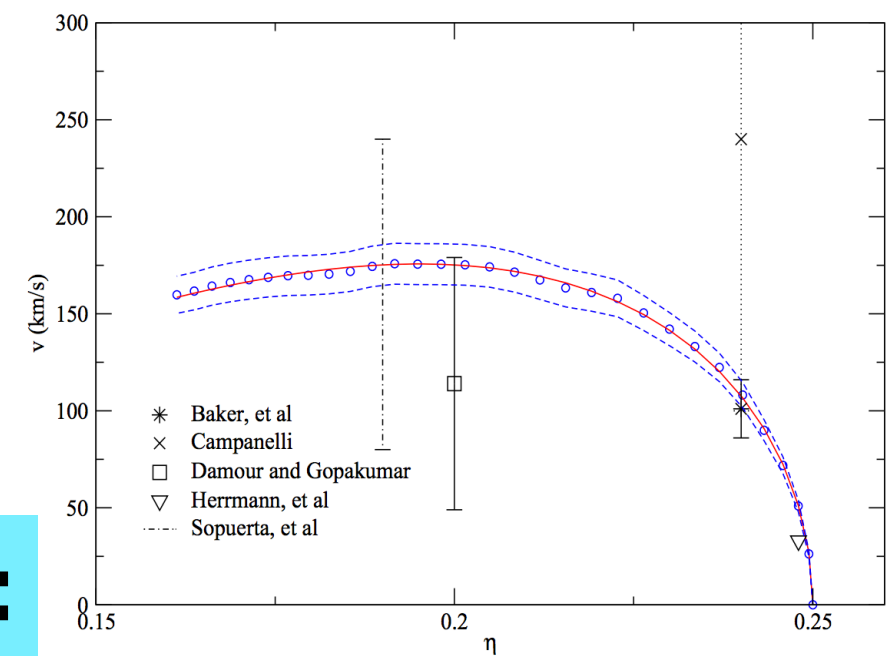


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**Competing project: SXS collaboration  
Calibration of Effective-One-Body models in time domain  
with long simulations, use spectral code.**

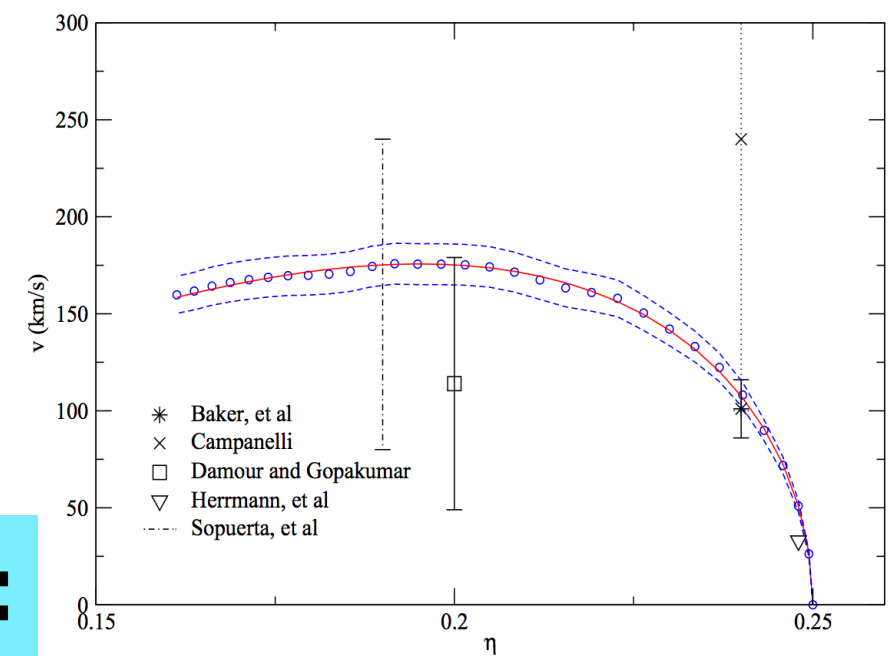
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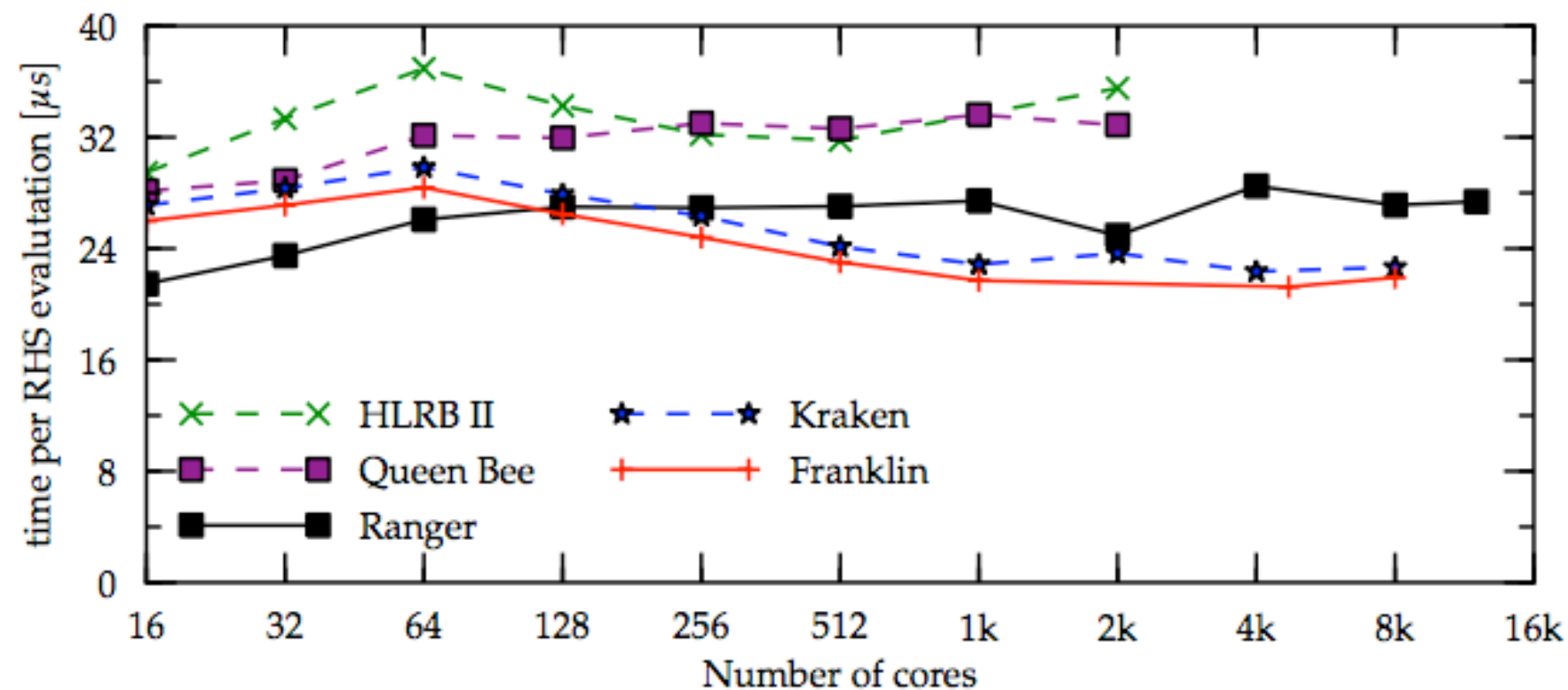
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# Code infrastructure

- Use 2 codes, use MPI and OpenMP domain decomposition parallelization:
  - BAM (developed originally at Uni Jena, C) - used for most production runs
  - Einstein toolkit (open source, C, C++, F90) - very active development
  - performance & scaling very similar
- Use explicit Runge-Kutta time-stepping: time step limited by Courant condition
  - Use ghost-point based variant of Berger-Oliger to refine temporal and spatial resolution.
- Outer grids dominate memory requirements, innermost grids speed.
- Checkpointing: longest simulation ran ~ 4 months.
- Run on the minimal number of cores for the problem, use available memory/core.

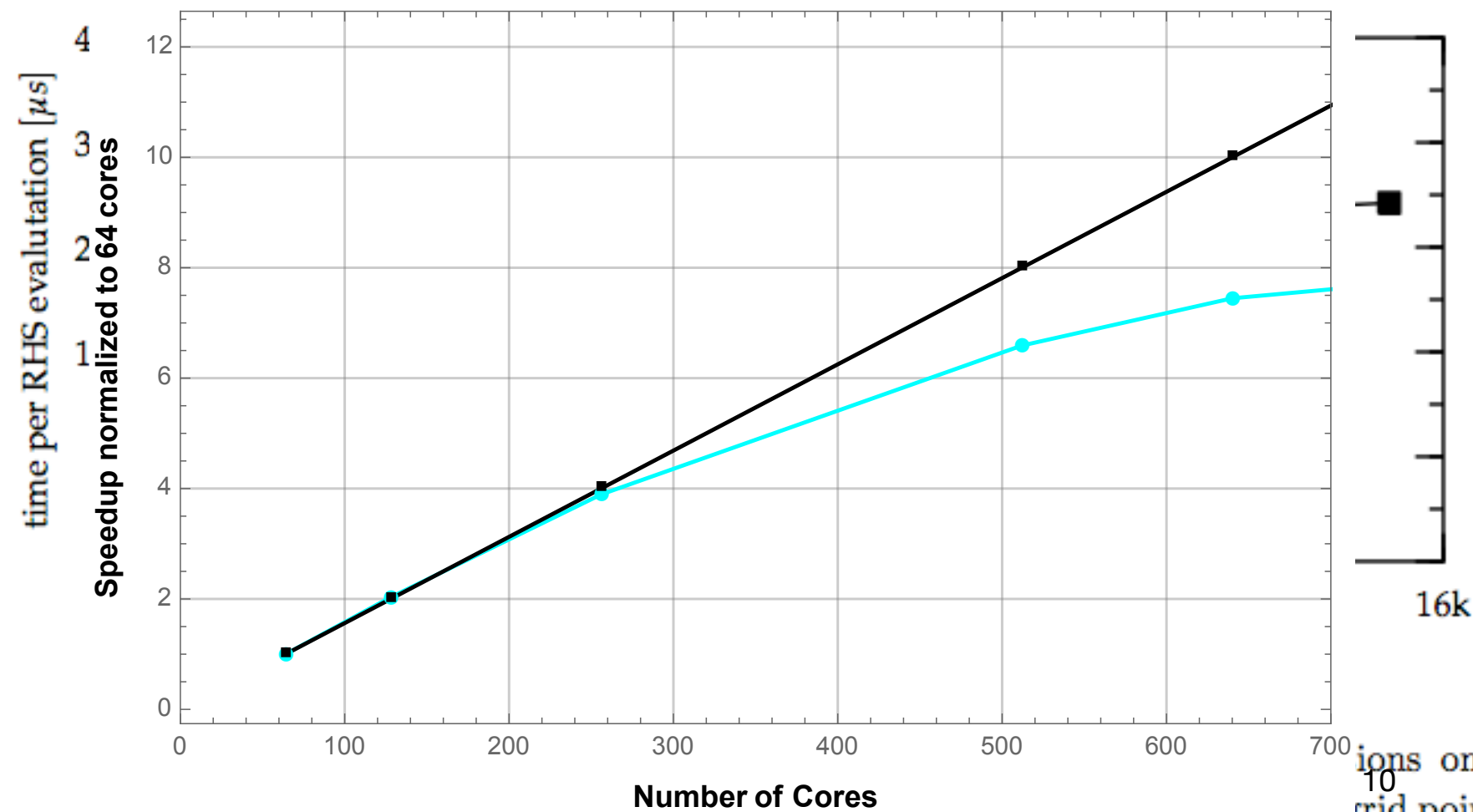


**Figure 2.** Results from weak scaling tests evolving the Einstein equations on refinement grid structure with nine levels. This shows the time required per grid point. Smaller numbers are better (the ideal scaling is a horizontal line). This demonstrates

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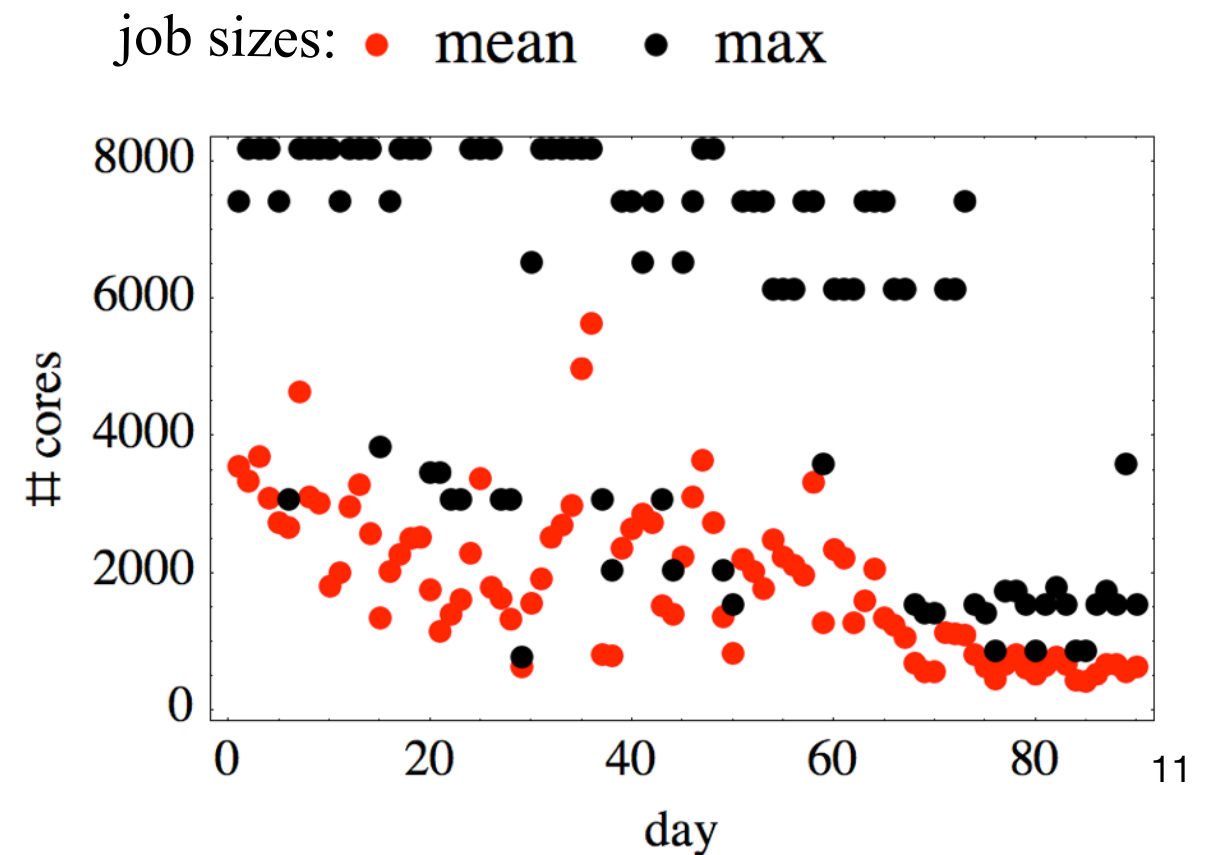
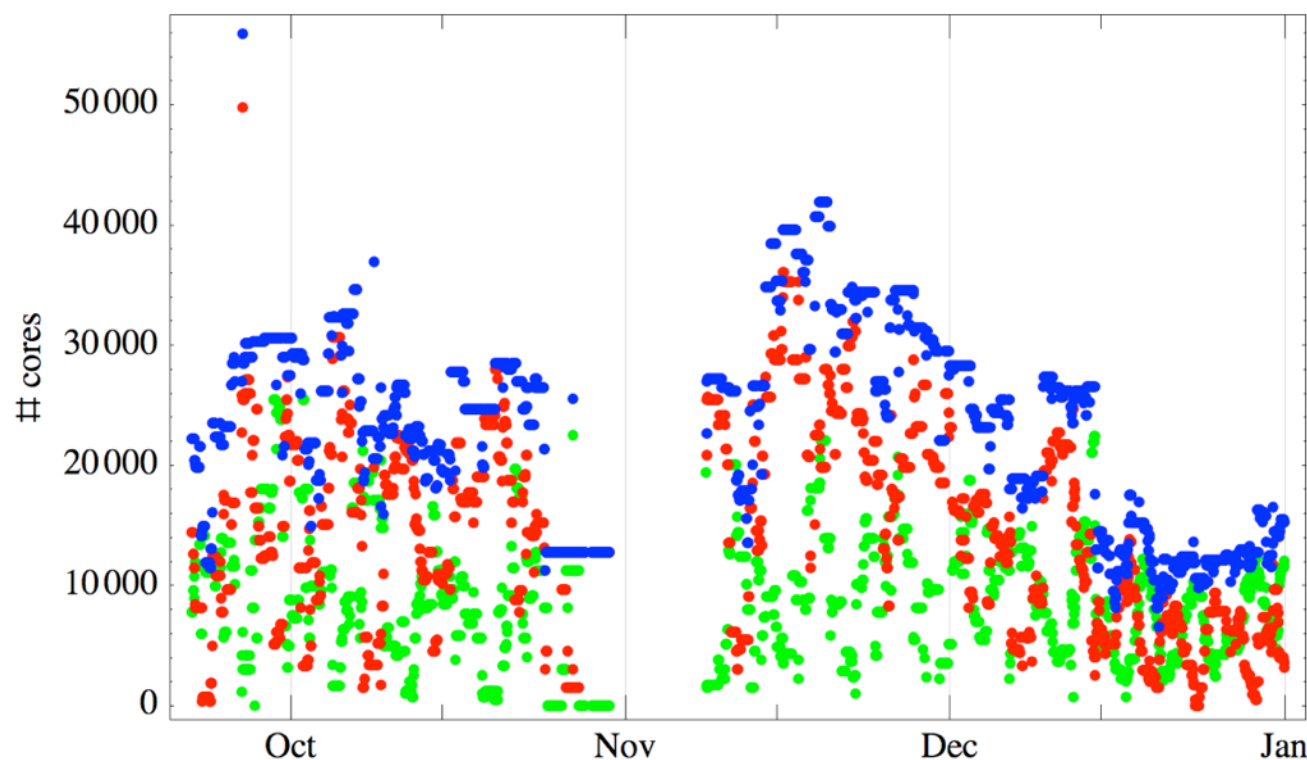




# Simulations performed & Job-bundling strategy

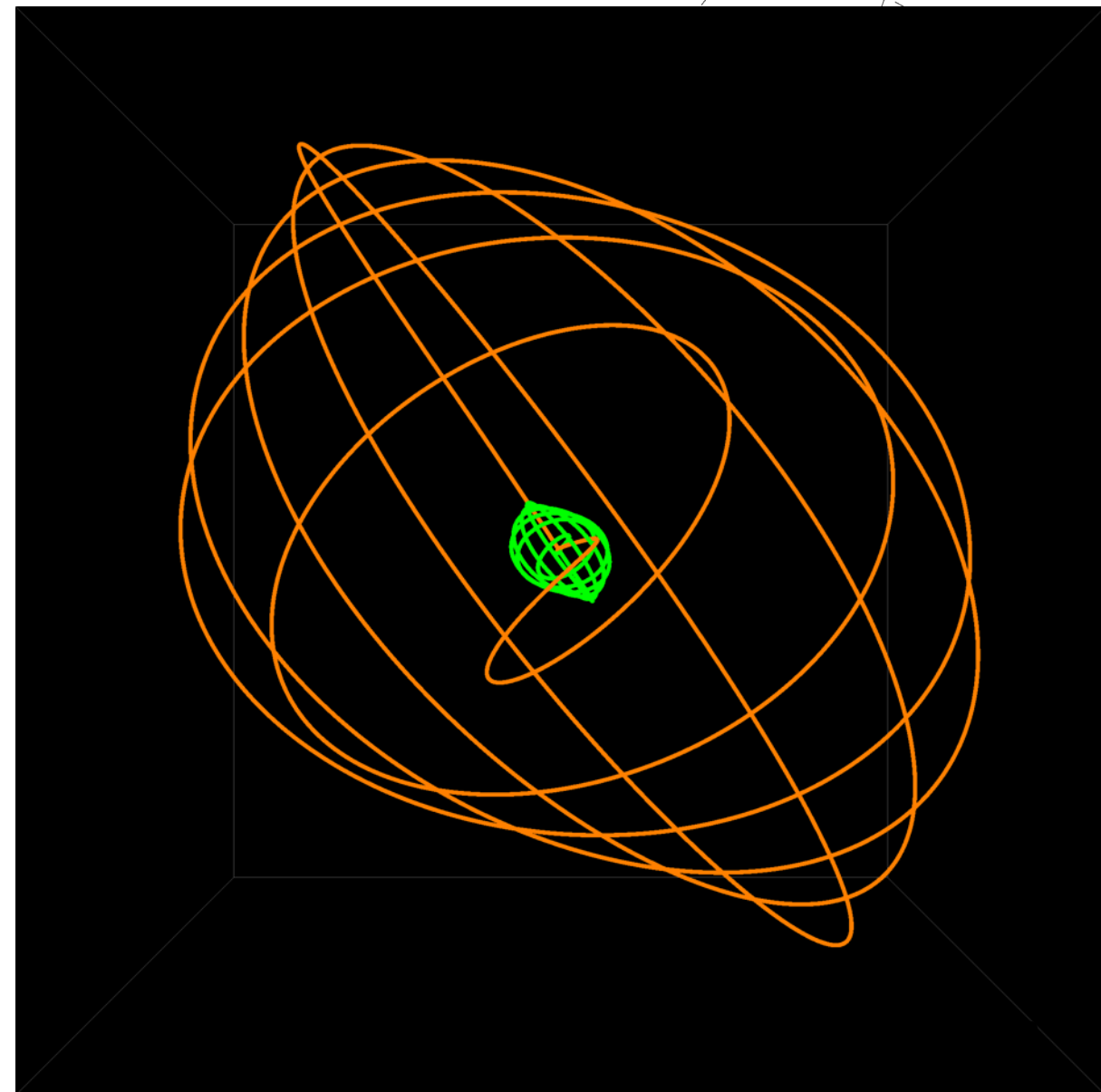
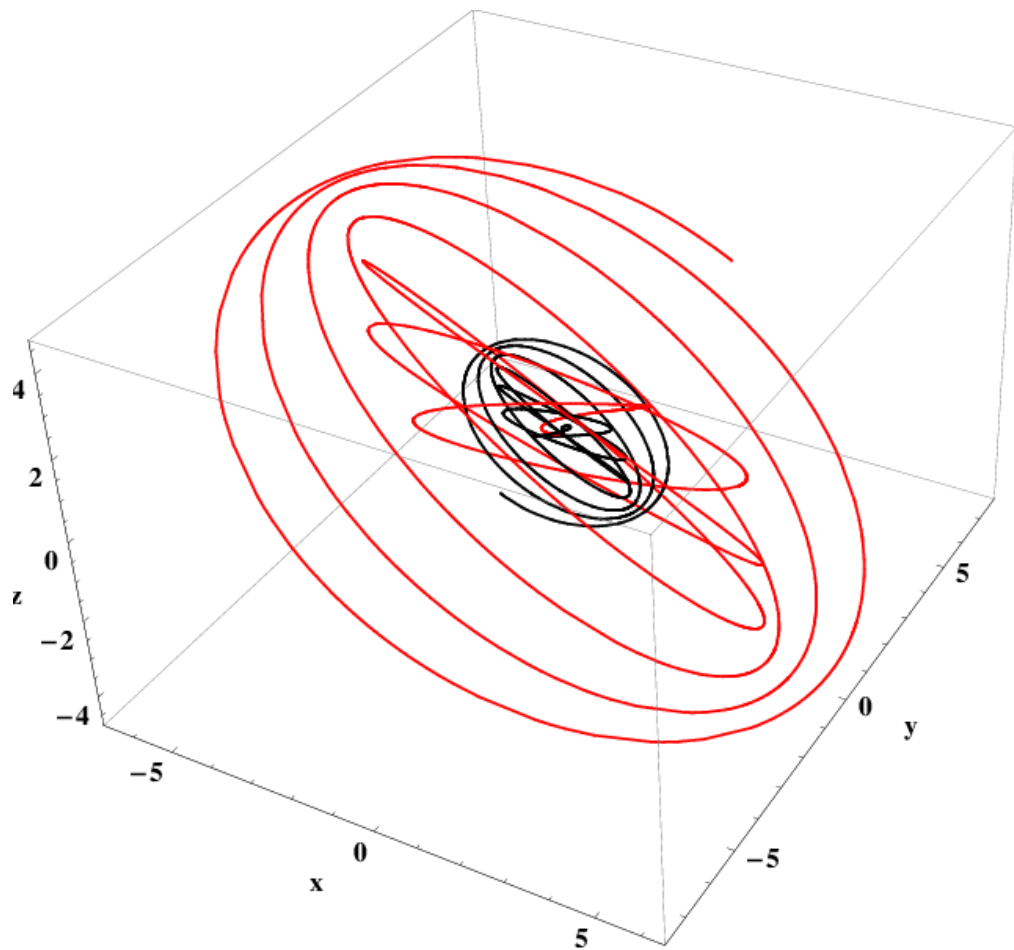
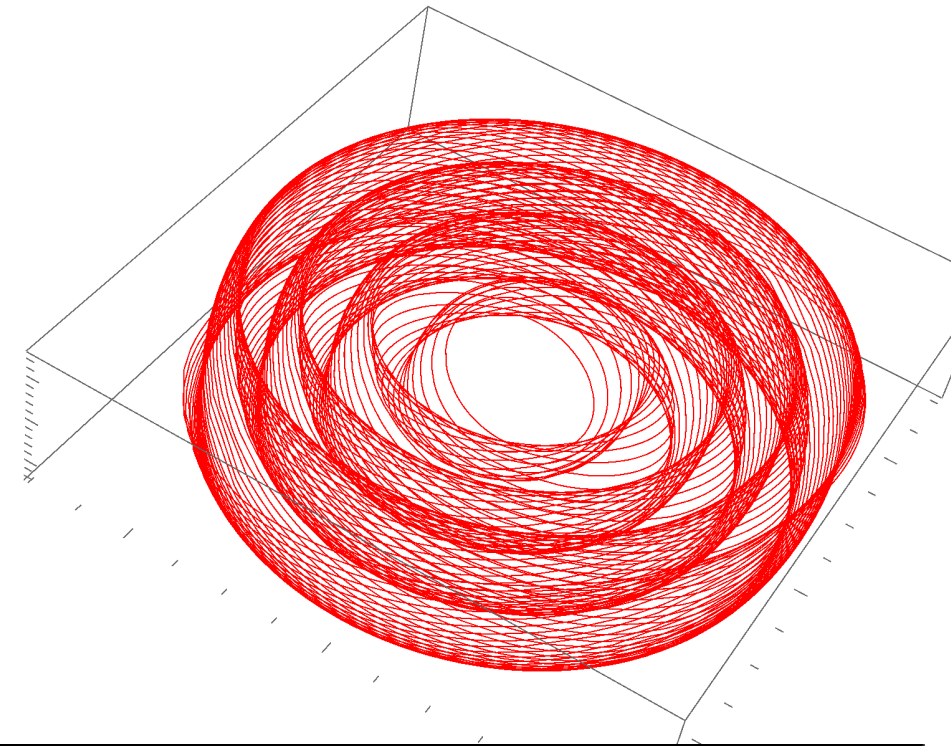
- PRACE-5: calibrate non-precessing model up to mass ratio 18, 37 million hours
- 12 high mass ratio cases: most expensive BH-simulations we are aware of  $> 10^6$  hours.
- Prepare large scale precessing study.
- Bundle several cases into bigger jobs, possibly reconfigure after each checkpoint.
- Monitor throughput, queue times, manage job chaining etc. with cron.
- LRZ provided workaround for bug in IBM parallel environment:
  - <https://www.lrz.de/services/compute/supermuc/loadleveler/special/index.html#subjobs-intel>
- Used  $> 20$  million hours during last ~4 months of allocation.

average cores running/queued/total=8 862/1 495/23 457



# The Challenge of Precession

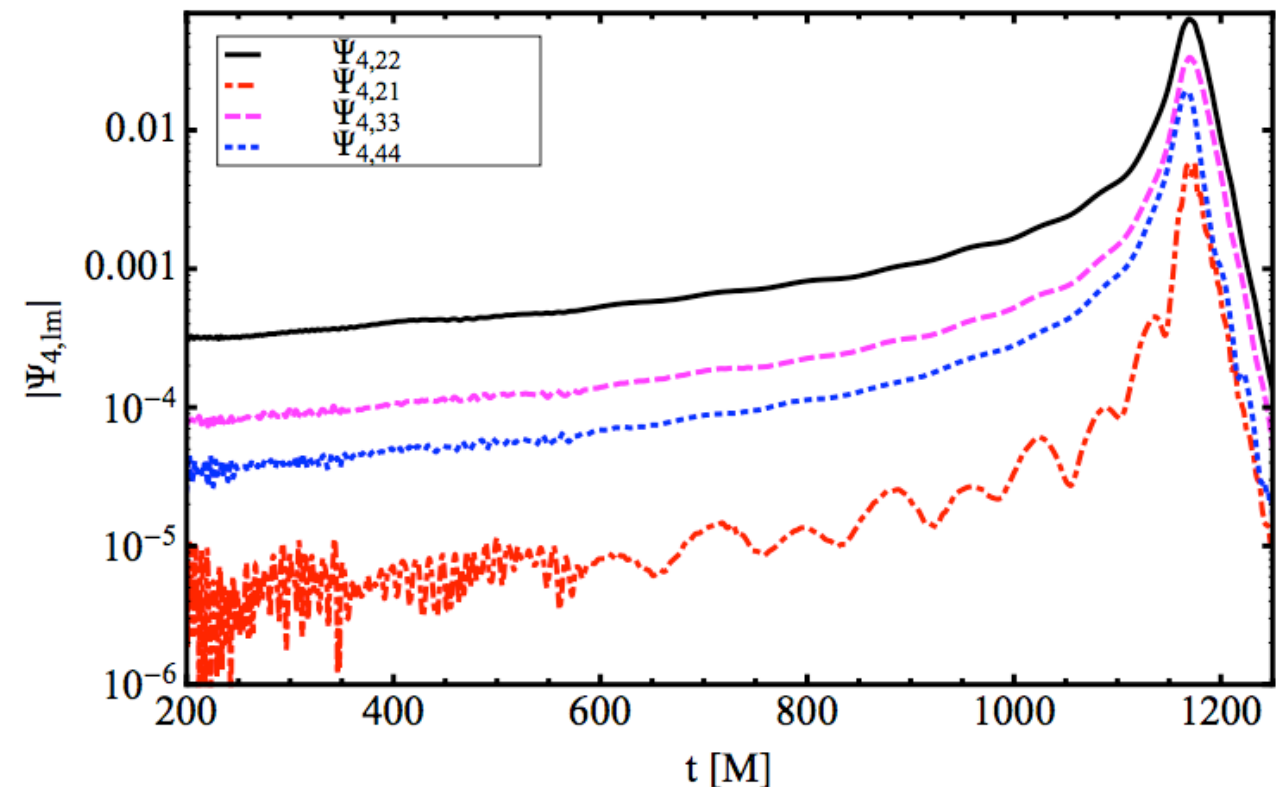
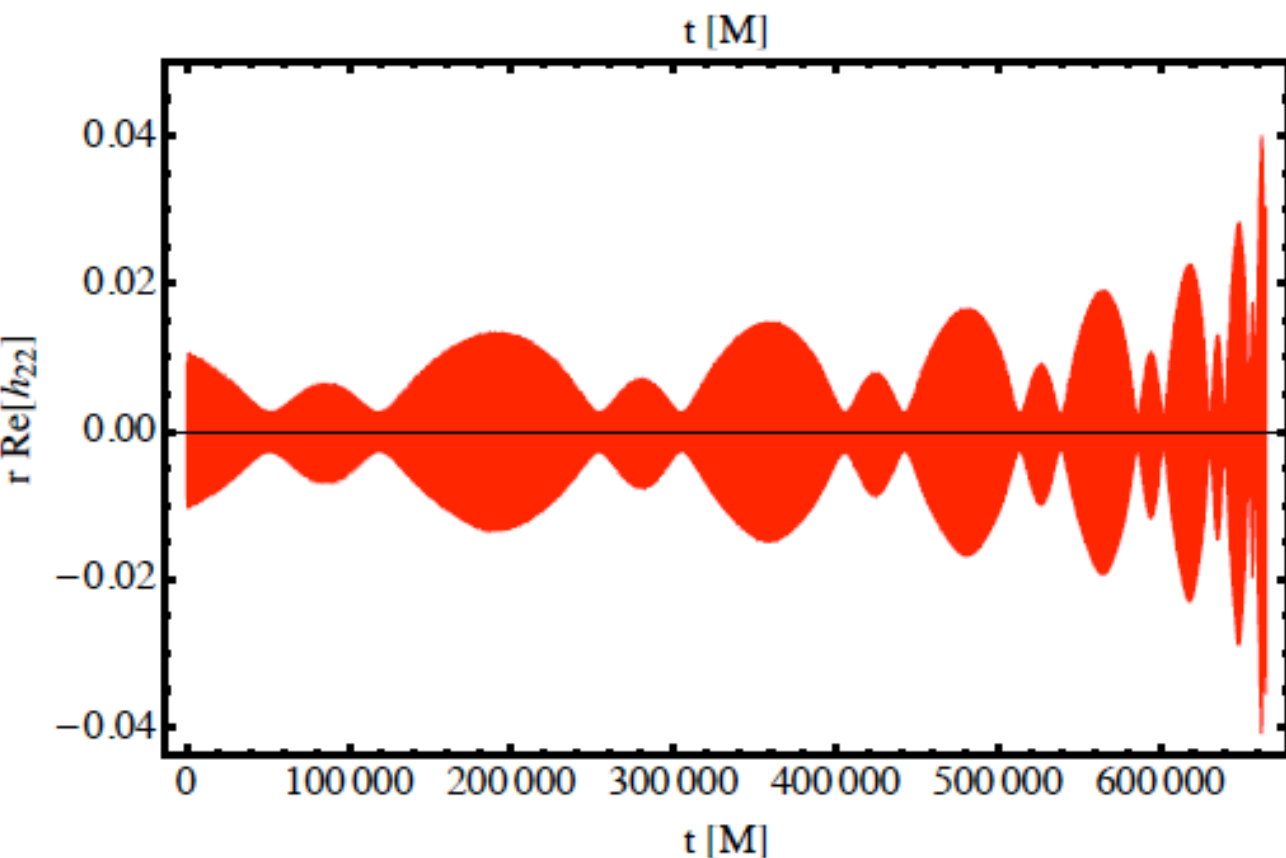
- Spins parallel to orbital angular momentum: no precession, orbital plane preserved.
- Orbital angular momentum and individual spins slowly precess around total angular momentum.





# A path toward understanding precession

- In a co-rotating frame the phasing and radiated angular momentum are essentially unaffected by precession - “simple standard form” of a precessing WF: align z-axis with principal axis of the radiation quadrupole moment [Schmidt+ PRD 2011]
- Spherical harmonic mode structure in standard frame corresponds to non-precessing case -> “twisting up” accurate aligned spin model with “post-Newtonian” Euler angles works well [Schmidt+ PRD 2012, Hannam+ PRL 2013]

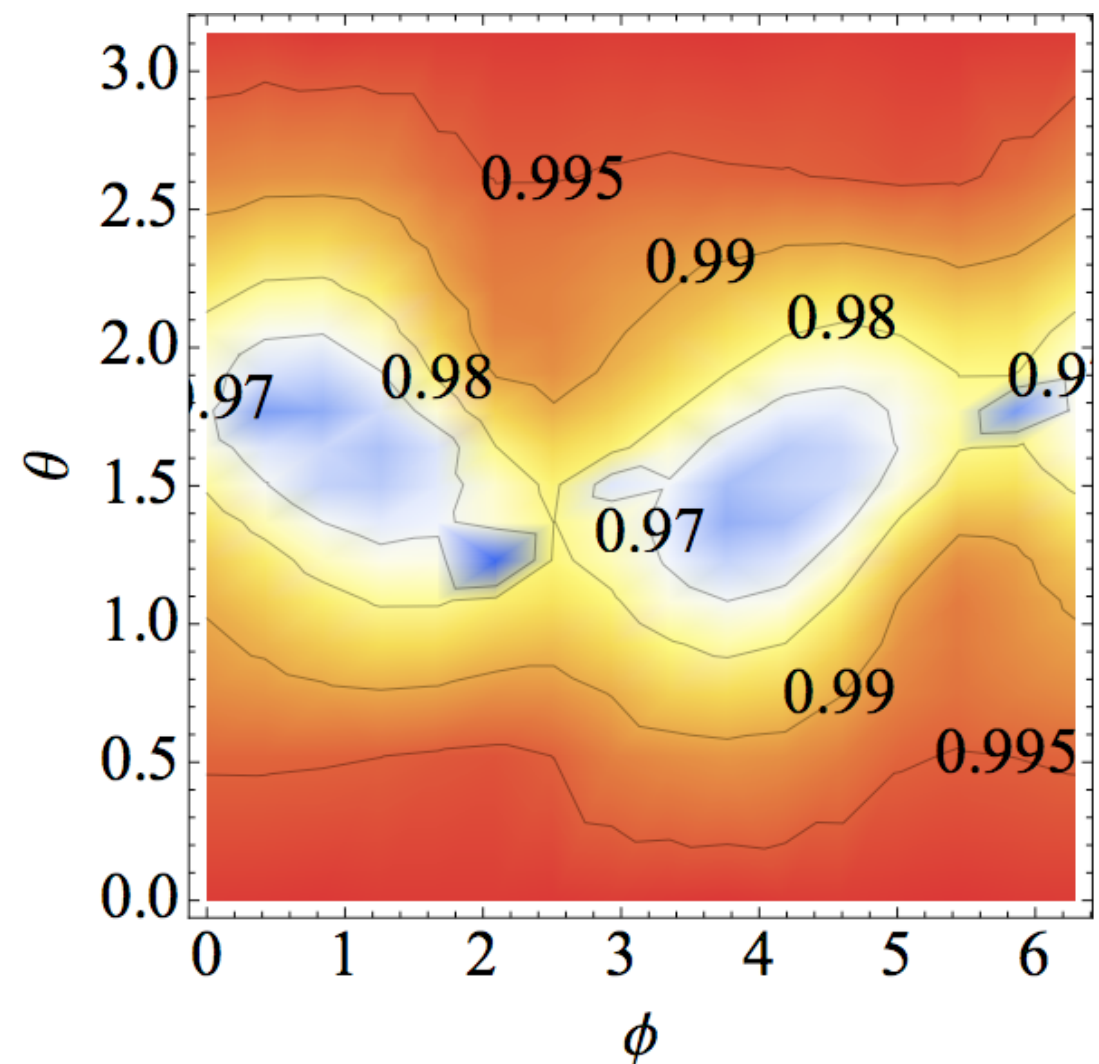
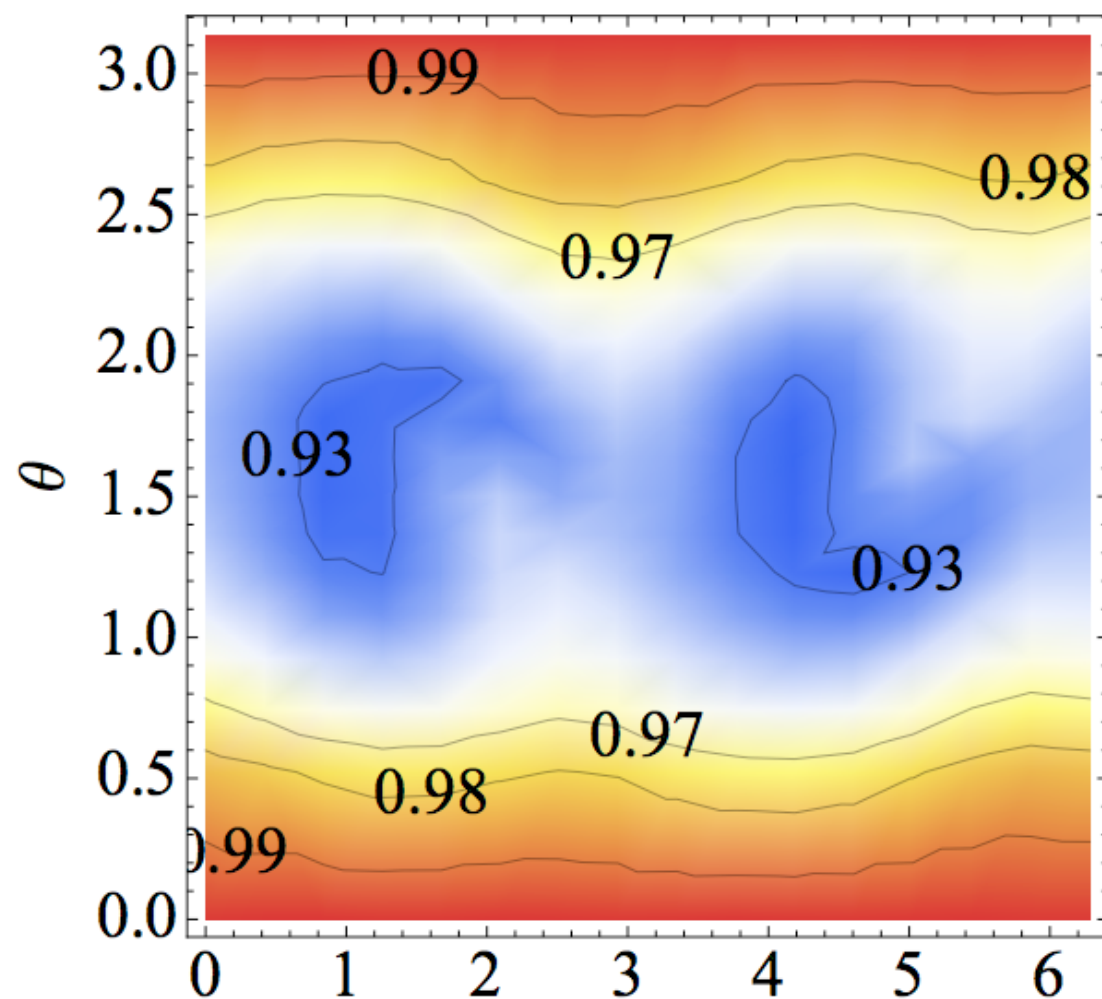


# Fitting factors: Models vs. PN-NR-hybrids

FF ~ detection efficiency: 0.97 standard detection limit

$$\langle h_1, h_2 \rangle = \max_{\phi_0, t_0} 4\Re \int_{f_1}^{f_2} \frac{\tilde{h}_1(f) \tilde{h}_2^*(f)}{S_n(f)} df$$

- PhenomC: nonprecessing model
- PhenomP: PhenomC twisted up with PN

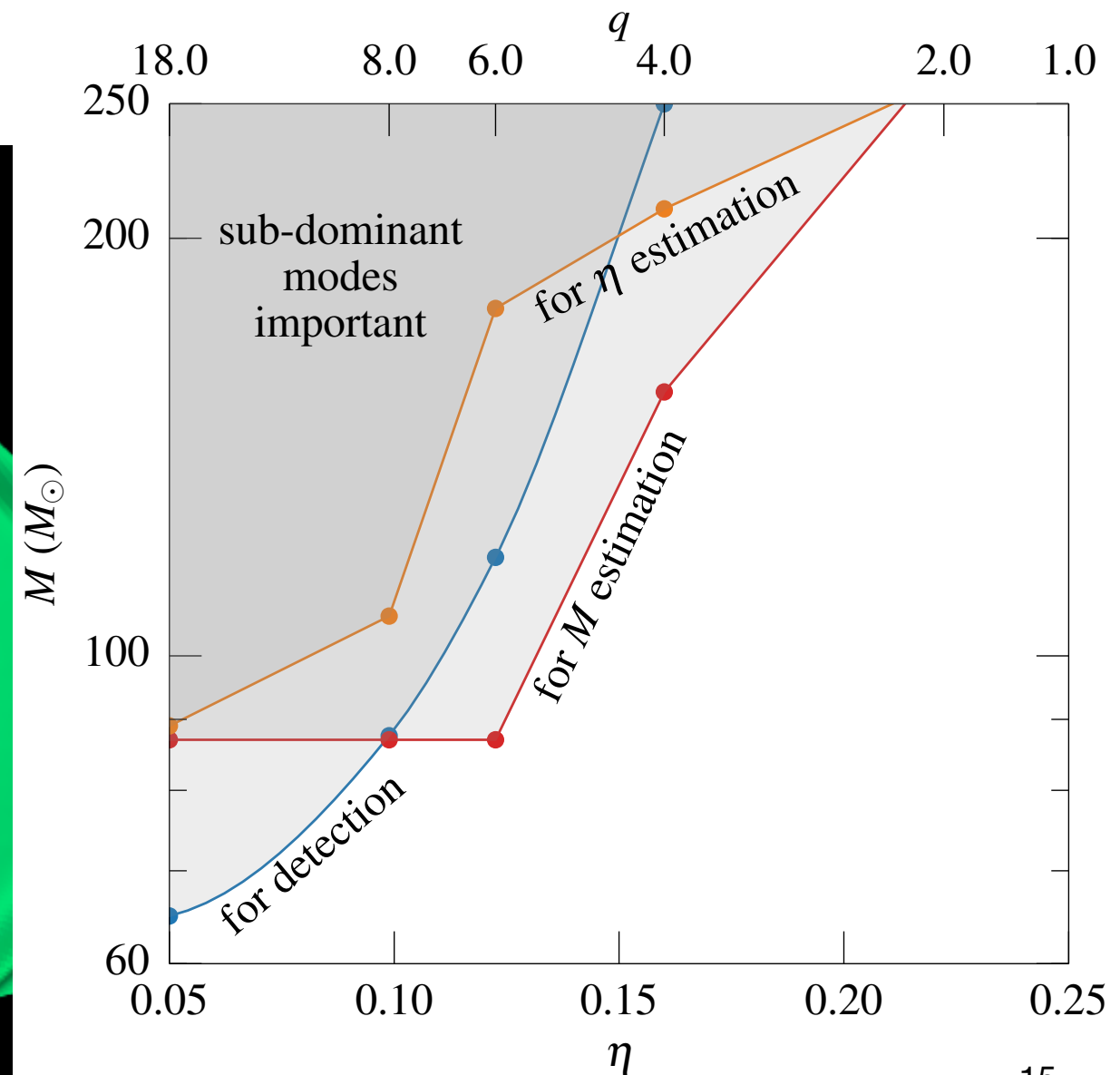
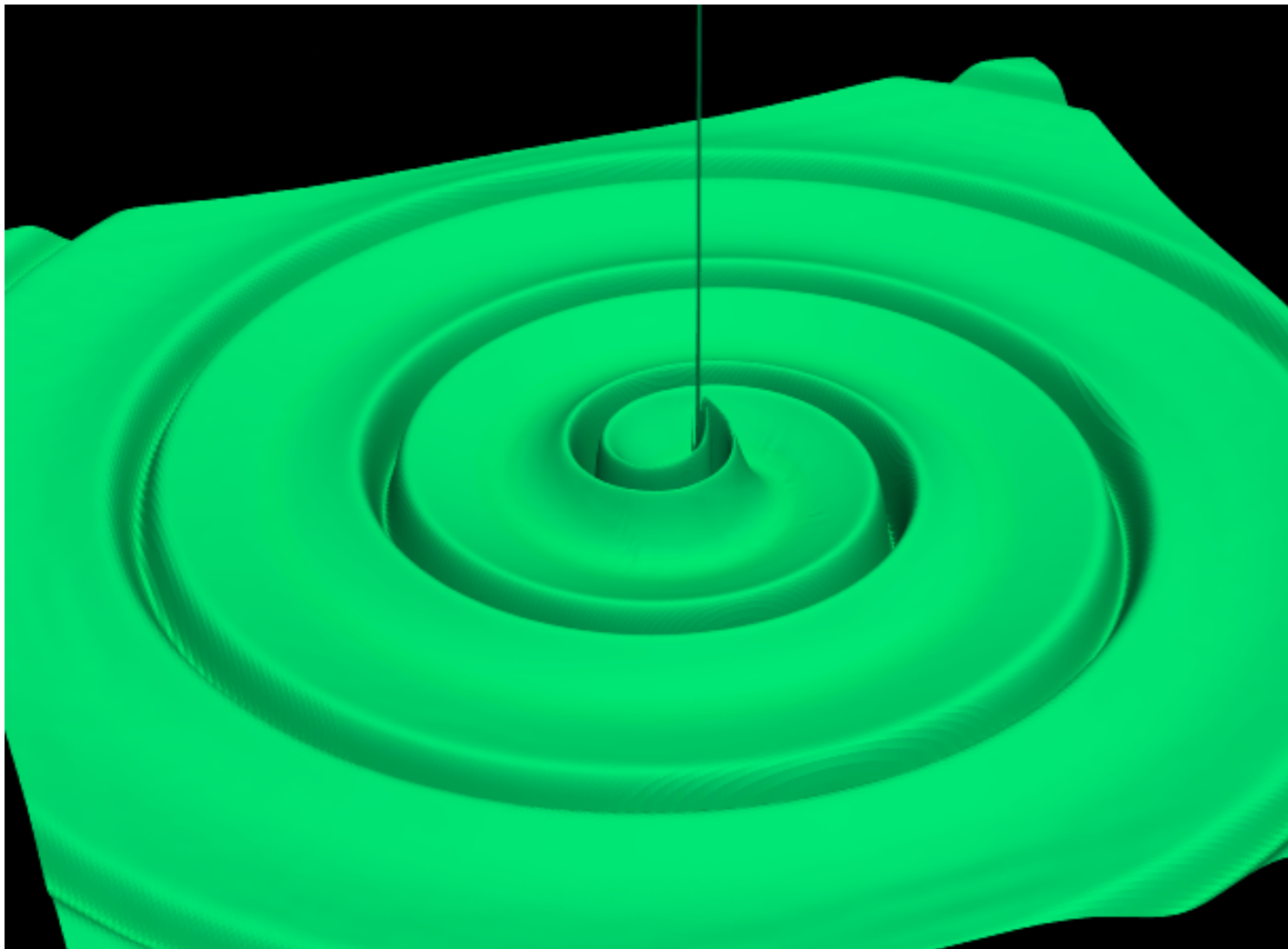


- Future: need to calibrate merger/ringdown to actual precessing NR waveforms.



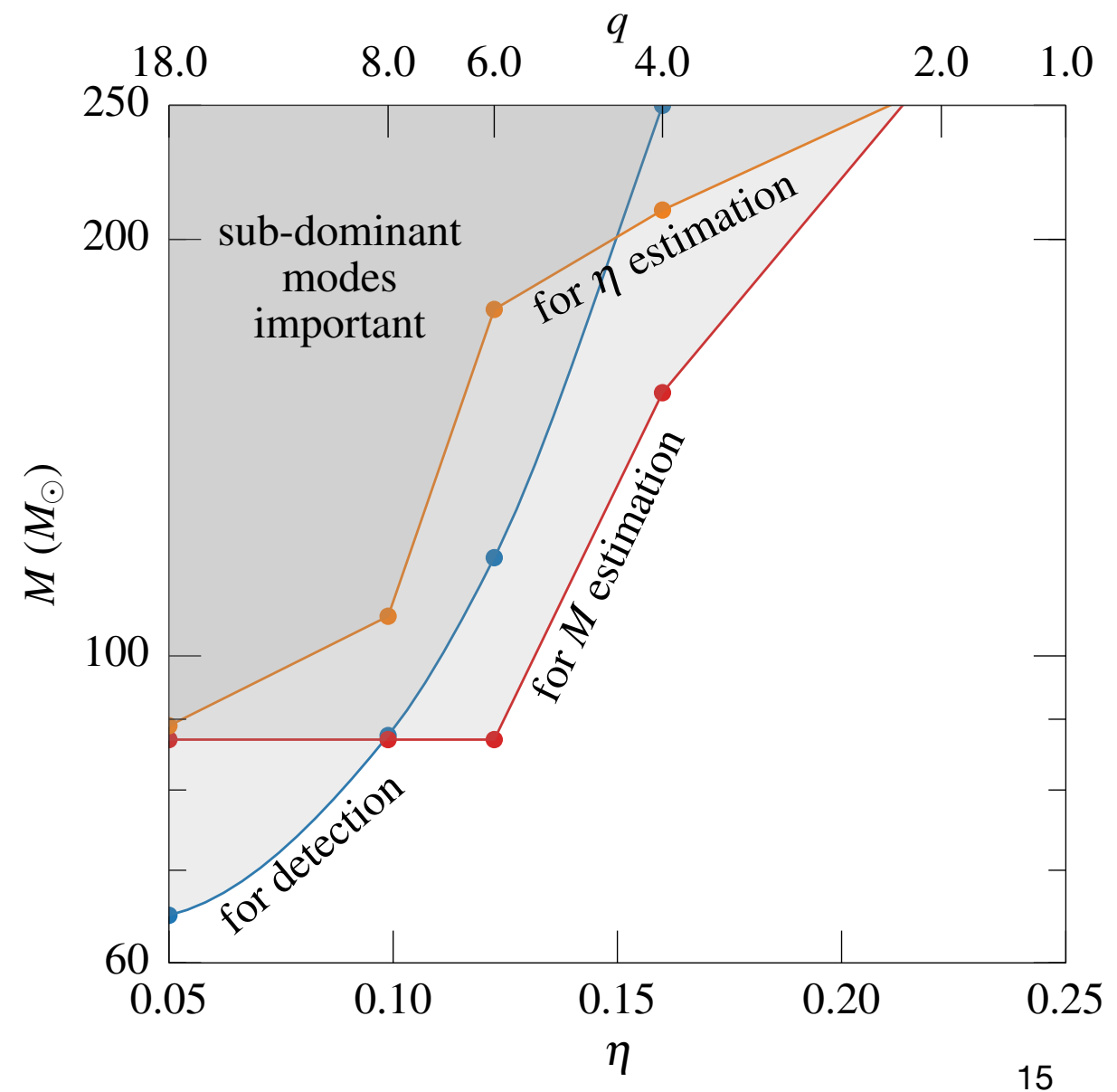
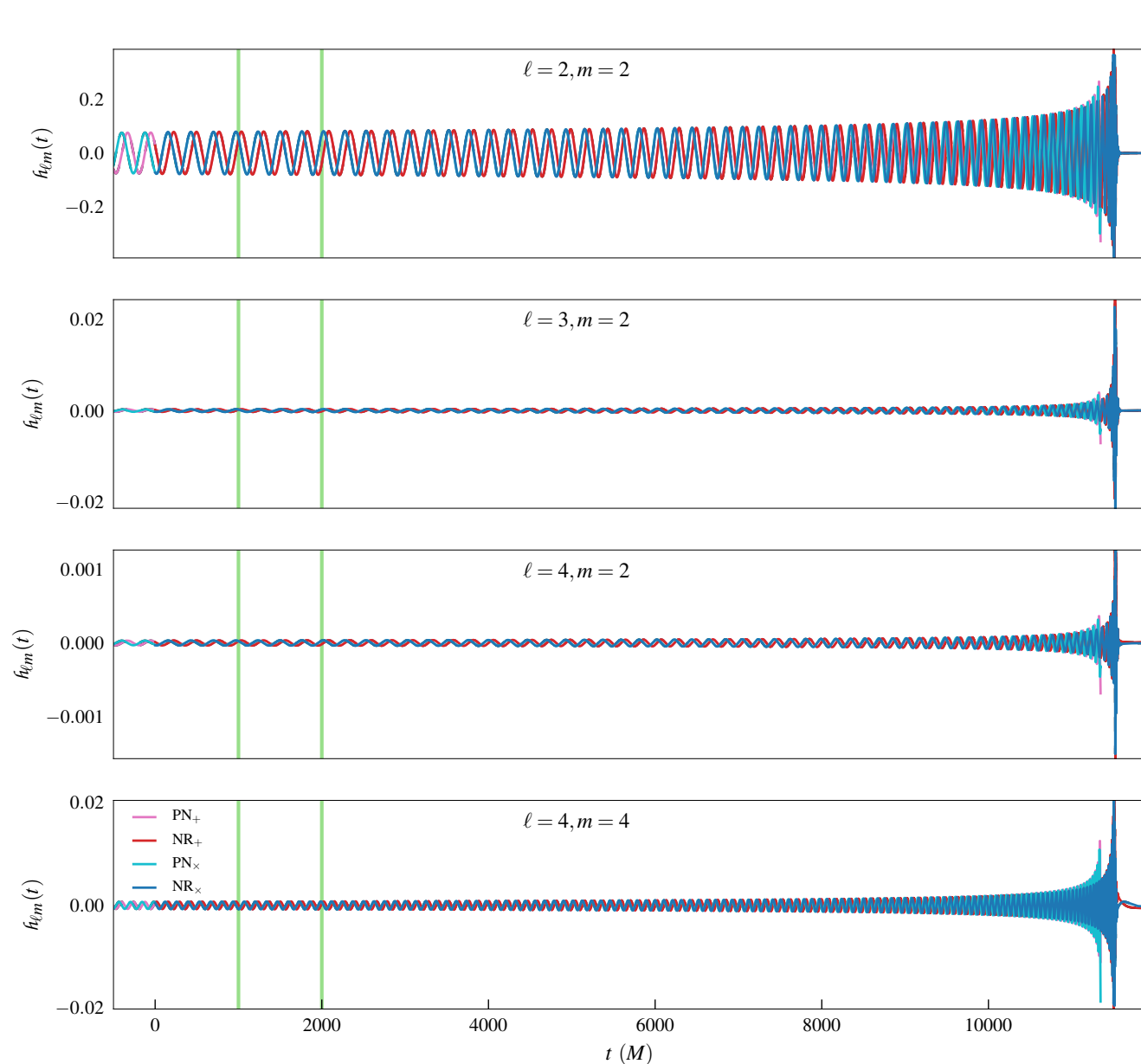
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- Understand where in parameter space higher modes are important when neglecting spin, starting to analyze general spinning case.



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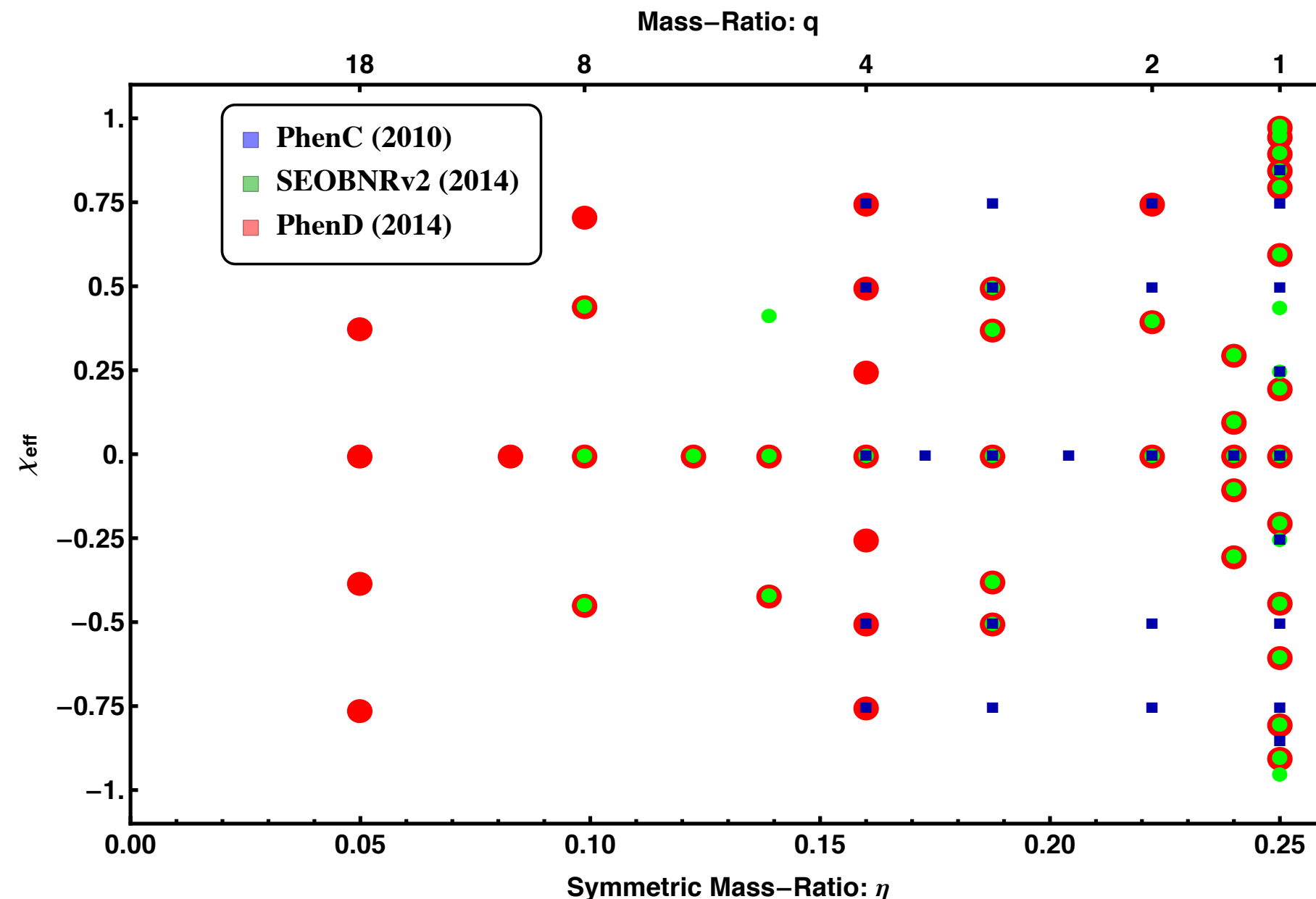
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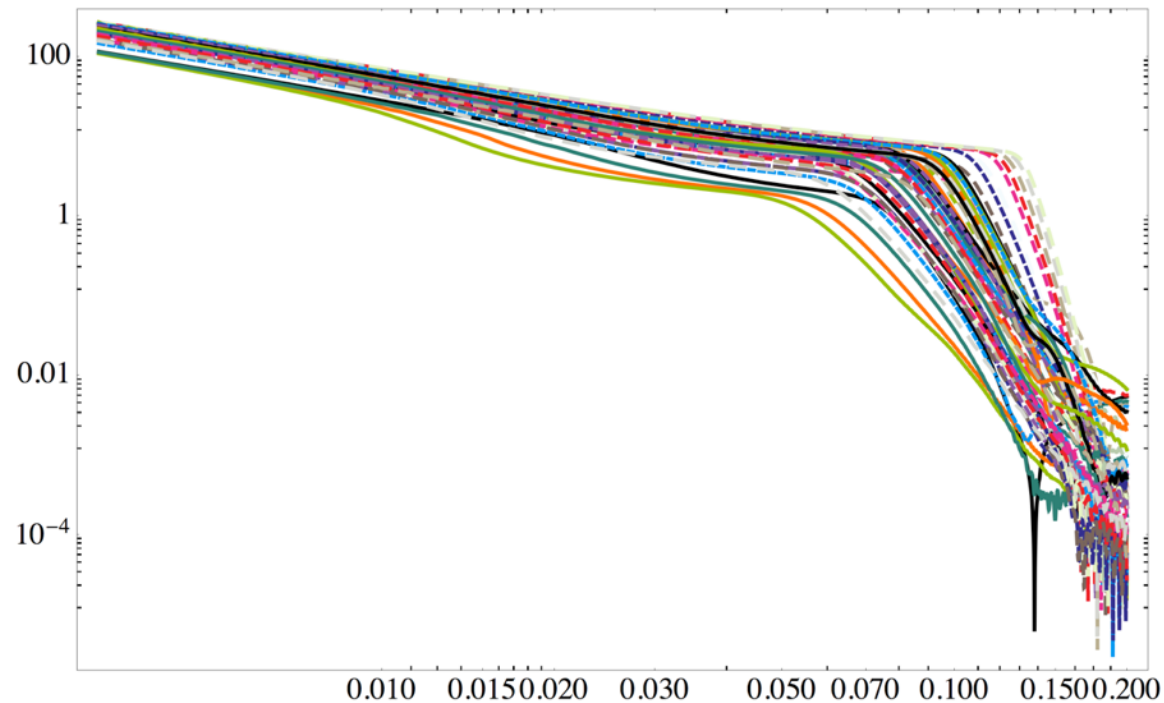
# PhenomD - Phenom re-imagined

- Currently used in GW data analysis: PhenomA/B/C/P
  - calibrated to  $m_1/m_2=4$ , moderate spins
    - want  $|\text{spins}| \sim 1$ ,  $m_1/m_2 \sim 100$
  - good for detection, parameter estimation “toy models”

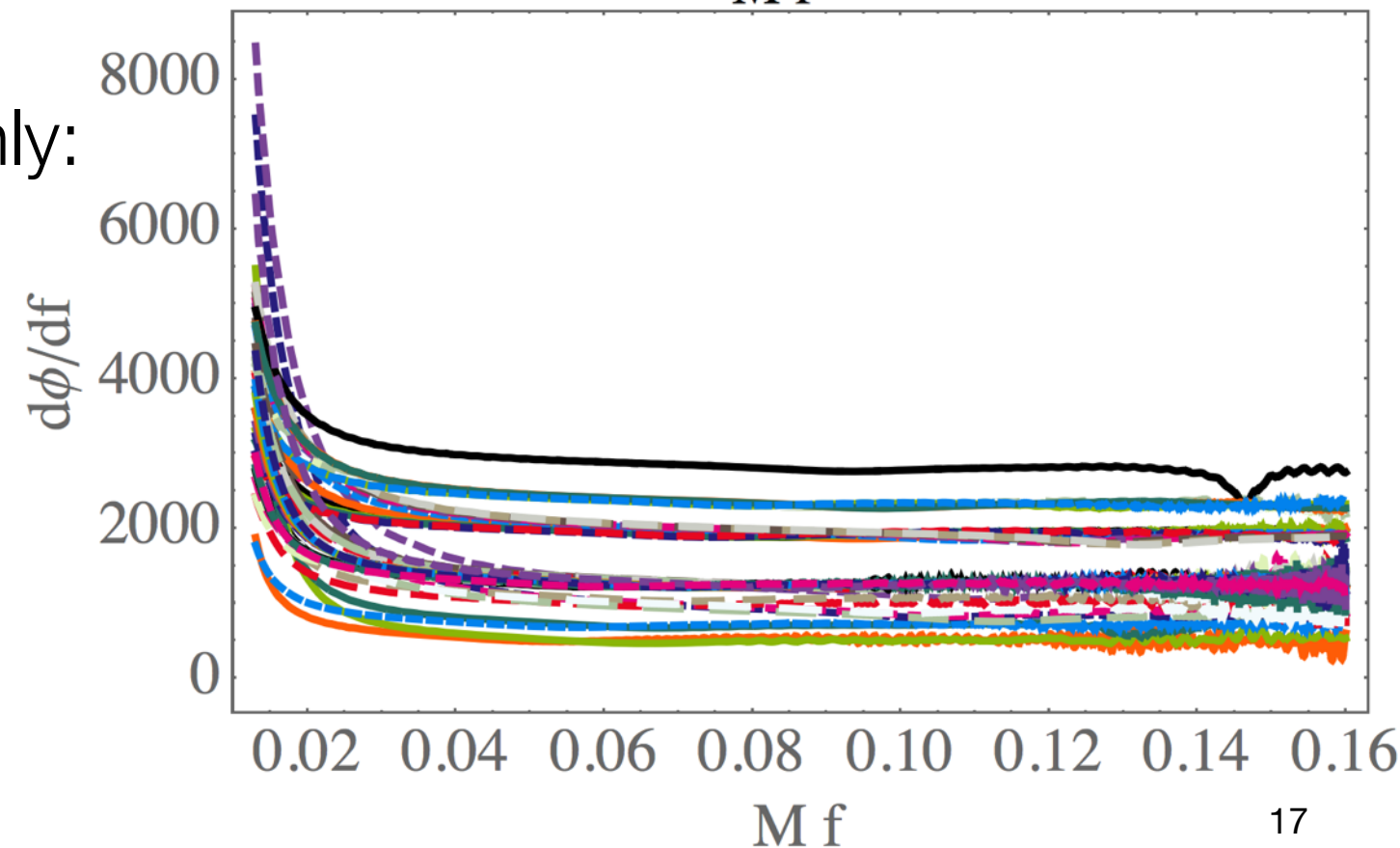
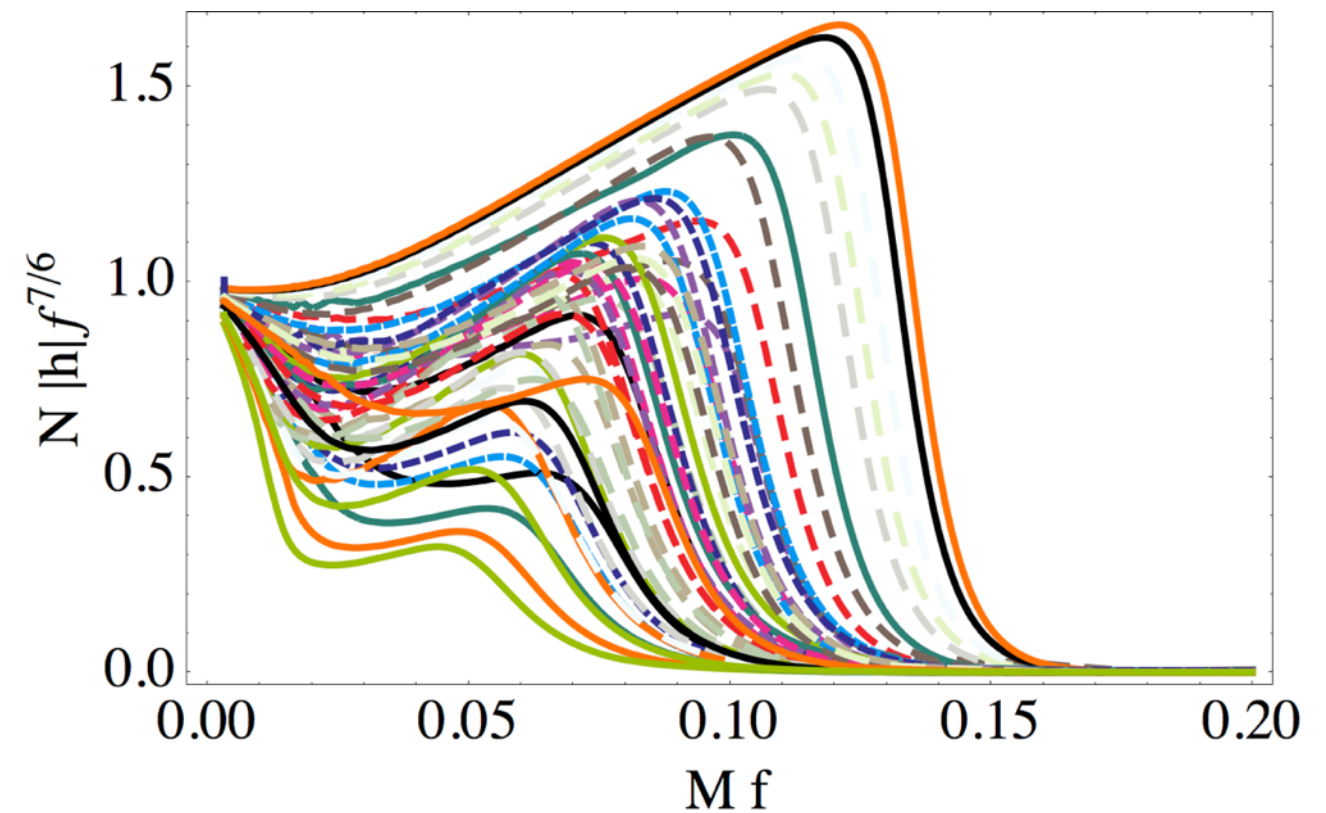


Based on non-precessing equal spin SXS & BAM simulations up to  $q=18$ .

# Raw data for modelling



- Dominant spherical harmonic only:  
 $l=2, |m|=2$
- Frequency domain  
amplitude & phase
- Model rescaled amplitude  
& phase derivative





# Phenomenological parameter fits

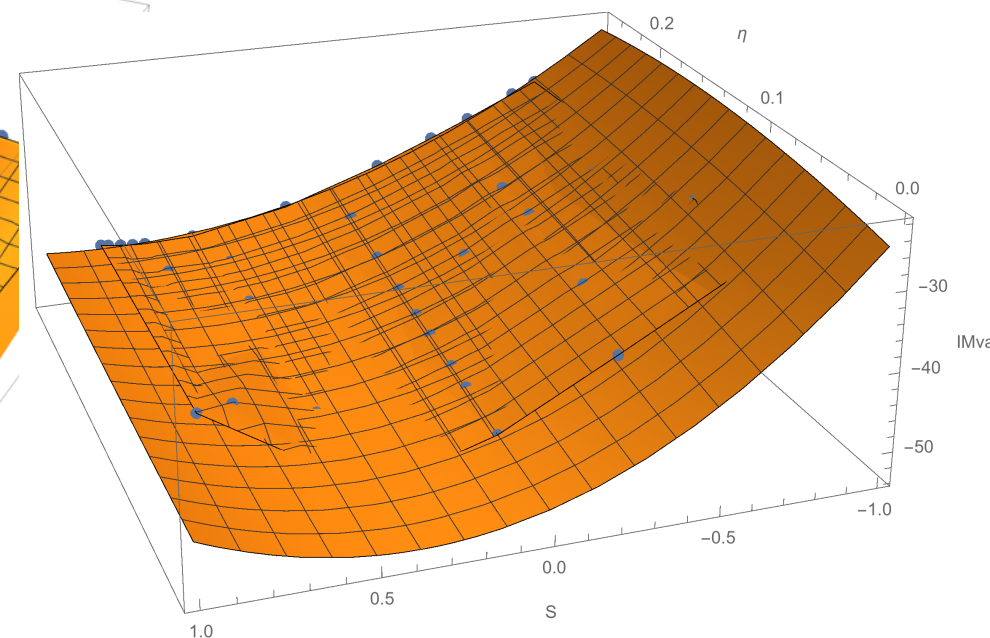
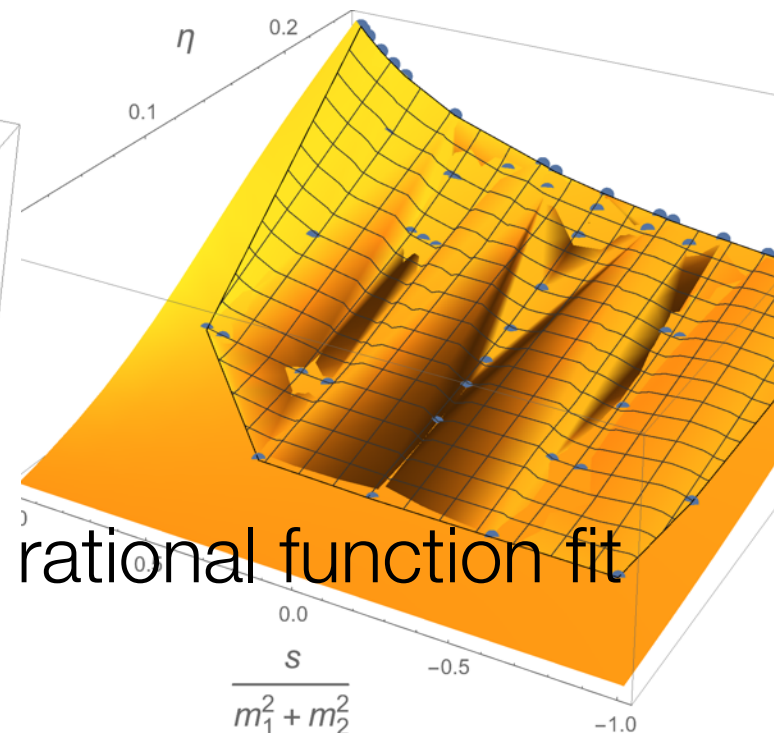
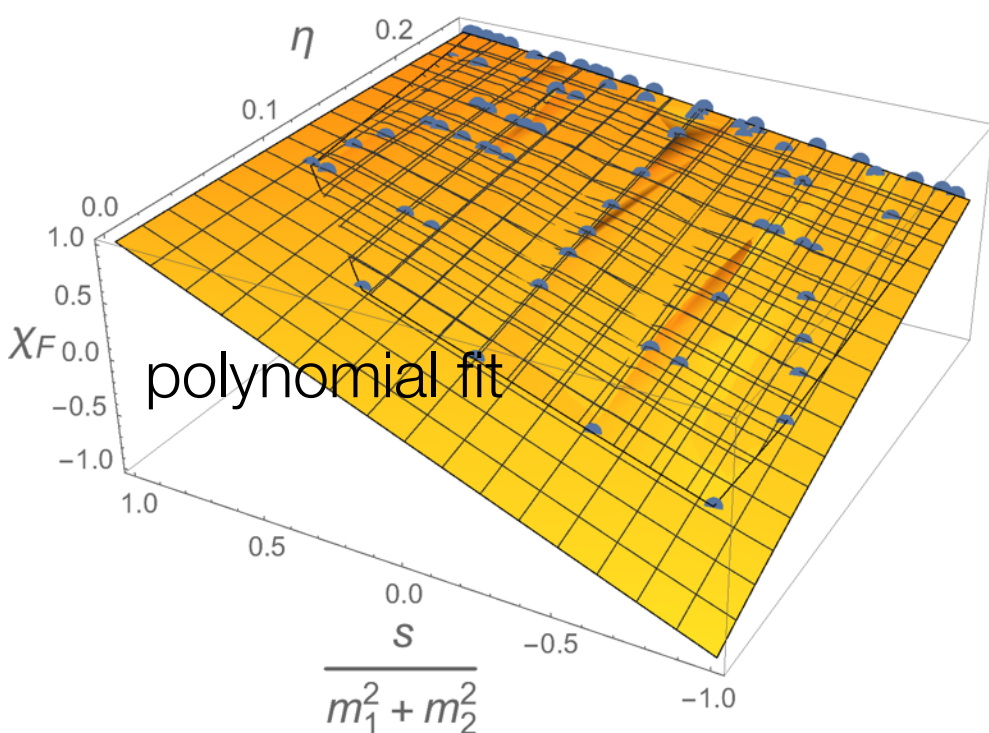
Example: merger/ringdown:

$$h_{MR} = \frac{ae^{-\lambda(f-f_{\text{ring}})}}{f_{\text{damp}}^2 + (f - f_{\text{ring}})^2} \quad \Phi'_{MR} = \alpha_1 + \alpha_2 f^{-2} + \alpha_3 f^{-1/4} + \frac{\alpha_4 f_{\text{damp}}}{f_{\text{damp}}^2 + (f - f_{\text{ring}})^2}$$

Total: 2 x 8-10 parameters as functions of  $(\eta, \chi_{eff})$

$$\eta = \frac{m_1 m_2}{(m_1 + m_2)^2}, \quad \chi_{eff} = \frac{m_1 \chi_1 + m_2 \chi_2}{m_1 + m_2} - \frac{76}{113} \frac{1}{2} (\chi_1 + \chi_2) \eta$$

P. Ajith, Phys. Rev. D 84, 084037 (2011)



# Phenomenological parameter fits

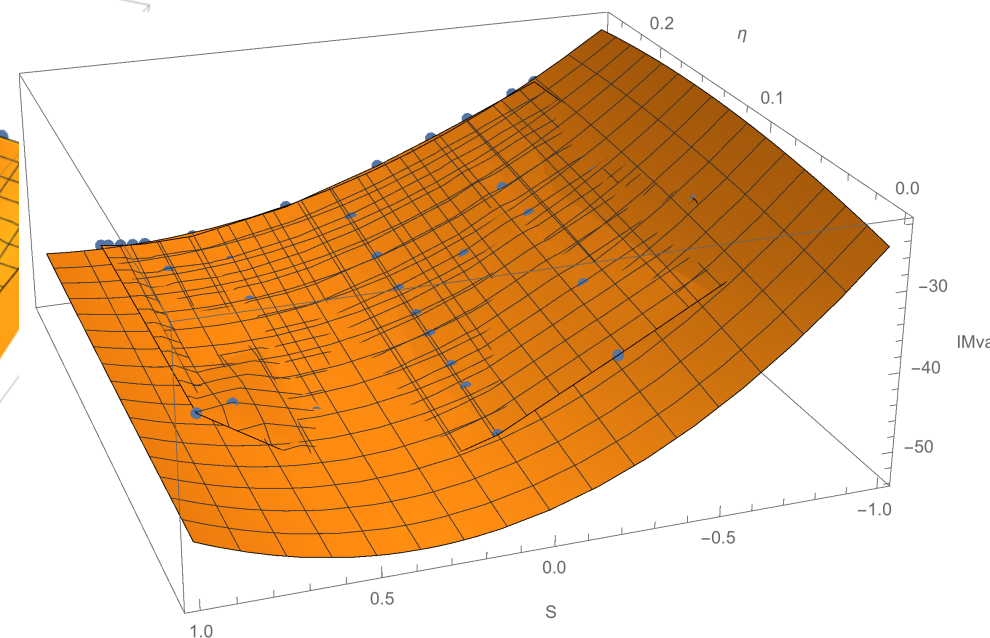
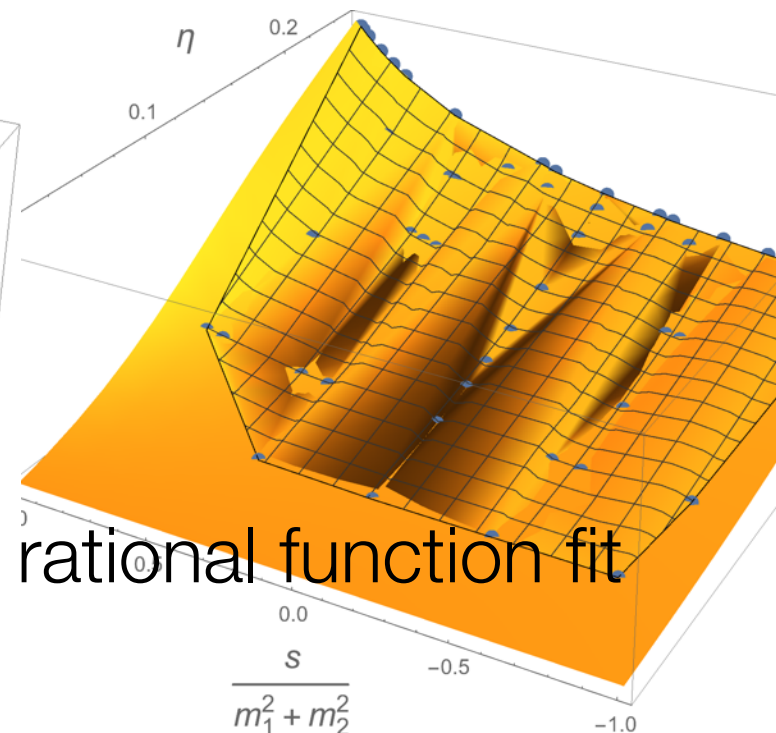
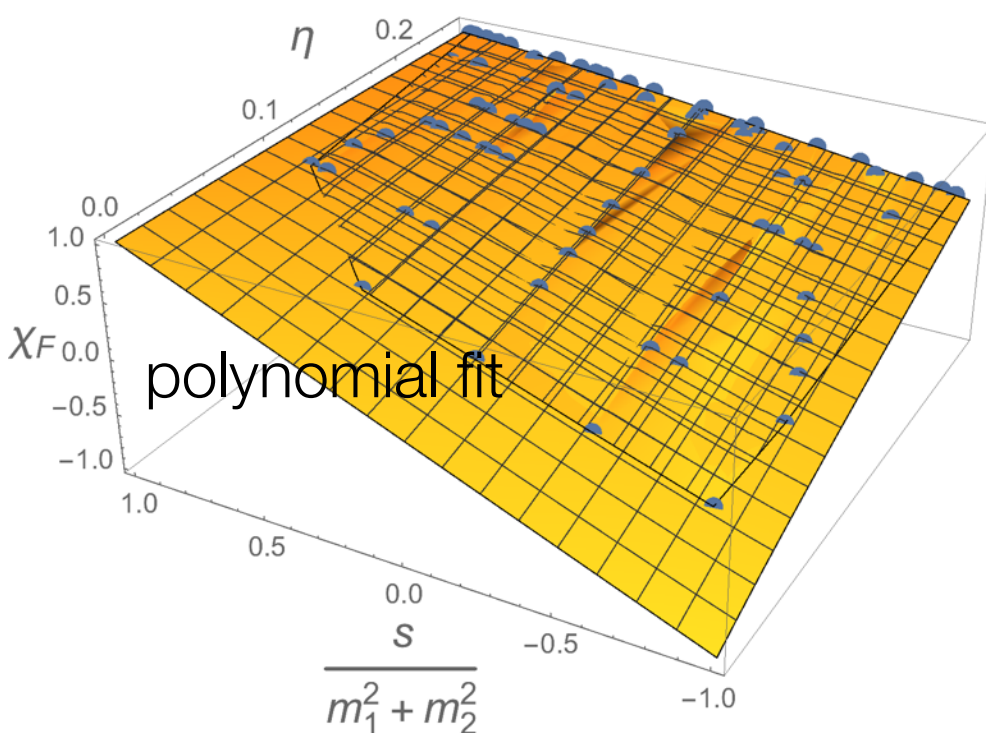
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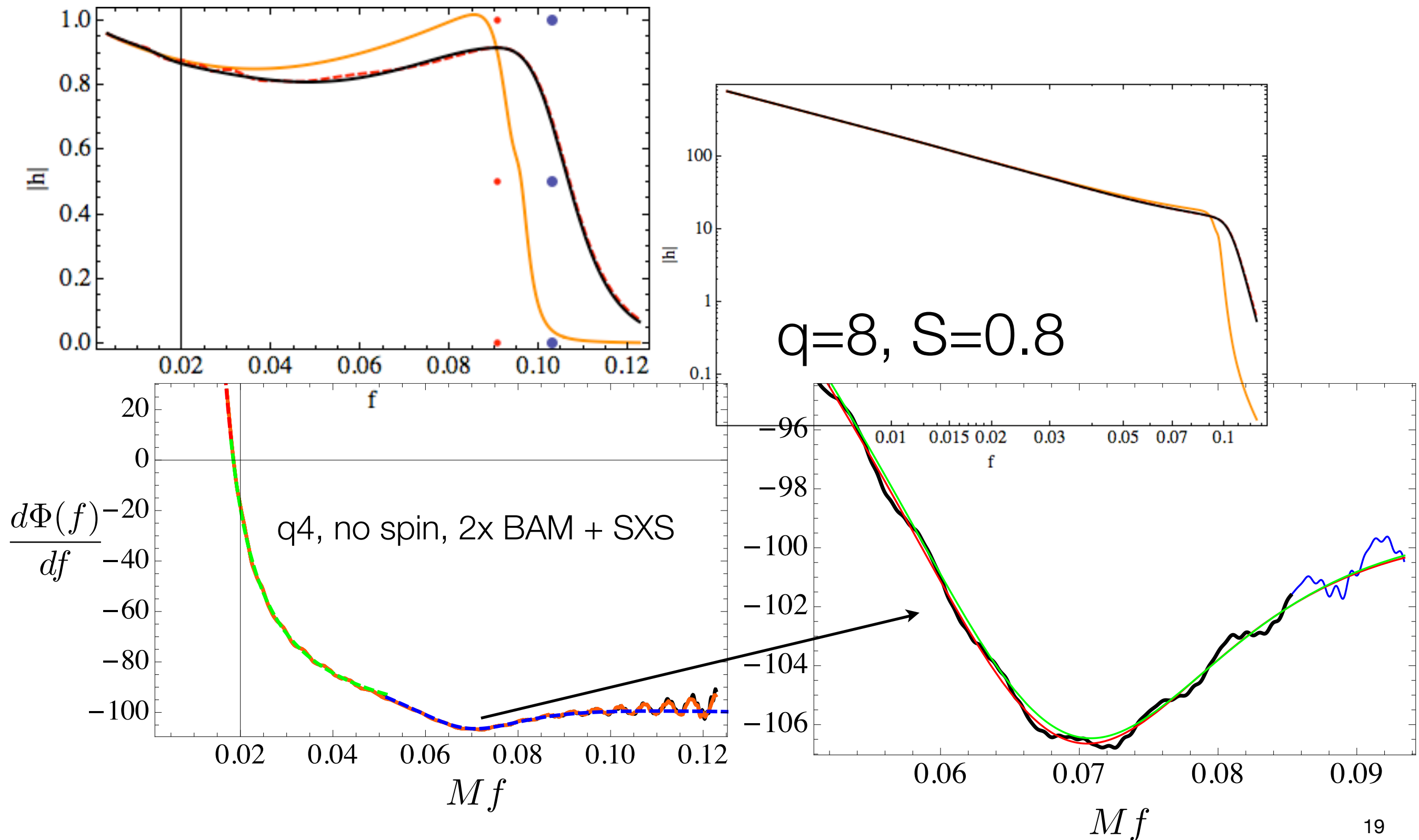
P. Ajith, Phys. Rev. D 84, 084037 (2011)



**Need more high spin data points**



# How well does this work: waveforms



# Matches vs. hybrids & between models

Nitz+ Phys. Rev. D 88, 124039 (2013)

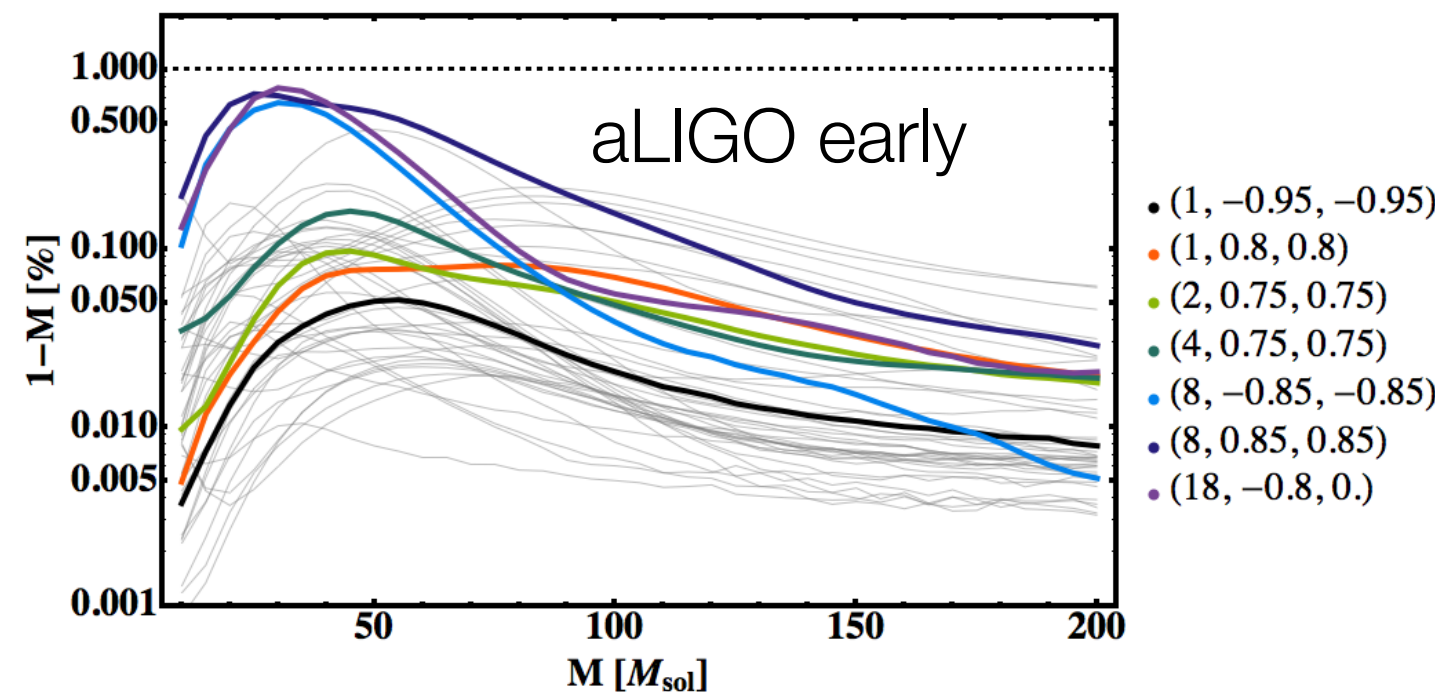
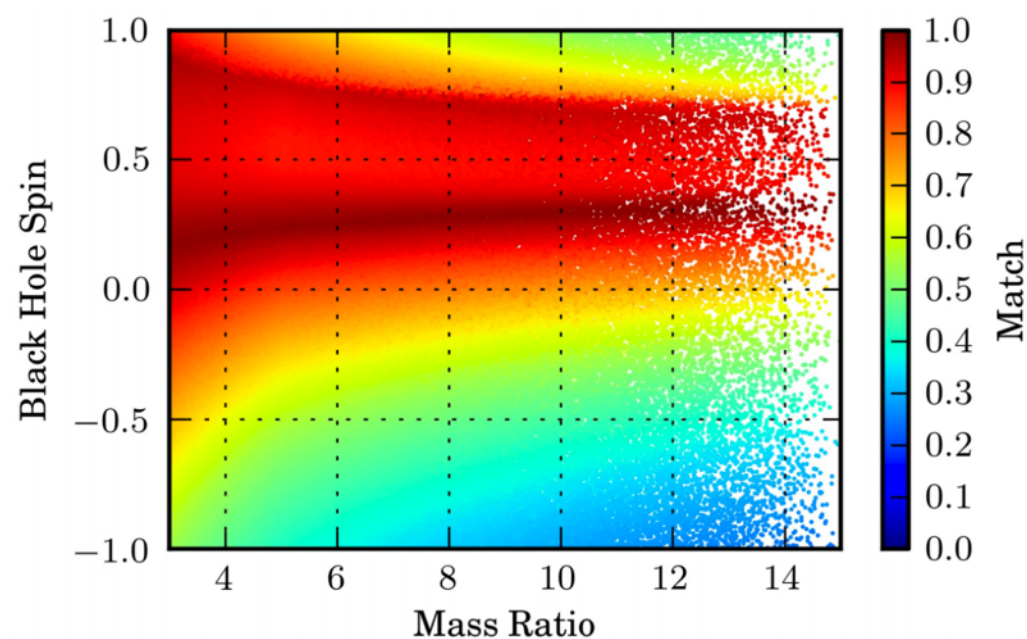
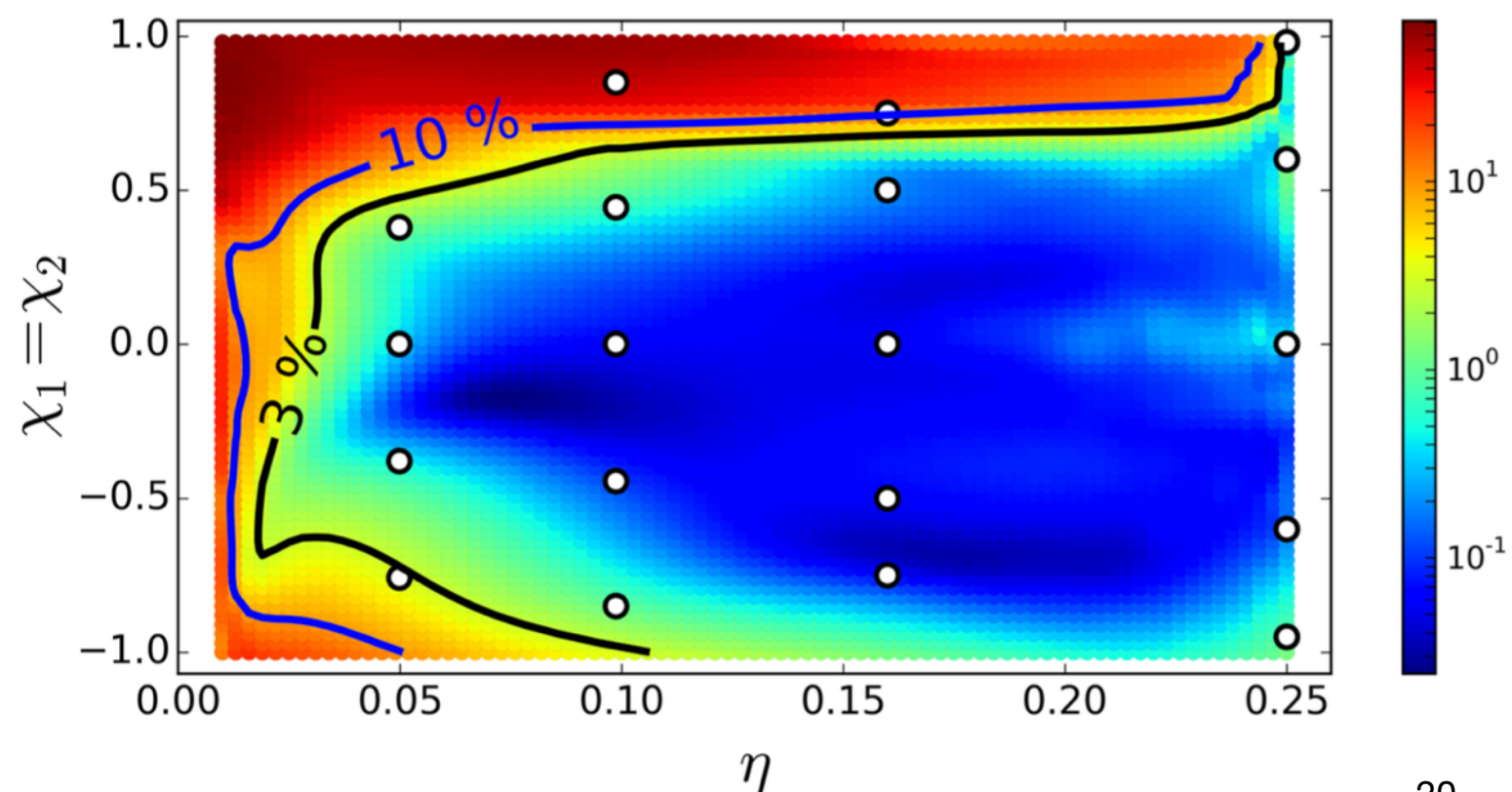


FIG. 16. The match TaylorF2 and TaylorT4 approximants, w. 3.5PN spin-orbit and 3.0PN spin-orbit tail corrections included a function of the spin of the black hole and the mass ratio system. The approximants include only the known spin terms 2.5PN. Matches are calculated using a 30Hz lower frequency to approximate the sensitivity of the early aLIGO detector. In



PhenD vs. SEOBNRv2



# Conclusions

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- Systematic study of highest mass ratio spinning BH mergers to date.
- Calibrated most accurate dominant mode non-precessing model to date.
  - Model accuracy drops significantly when BHs have large positive spins, astrophysical likely & “louder”.
  - —> further need for refinement
- Developed a plan to conquer precessing spin space.
  - supported by ERC Consolidating grant to Mark Hannam.
  - Technically ready to run 100s of precessing cases.
- Advanced GW detectors ready for first observing run 09/2015, 6-month run in 2016.
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